Software Verification Exercise: Data Flow Analysis

1 Reaching definitions analysis

Consider the following program fragment:

```
 \begin{array}{l} {\bf x} := 10 \\ {\bf while } {\bf x} > 0 \ {\bf do} \\ {\bf y} := 2 * {\bf y} \\ {\bf if } {\bf y} > 10 \ {\bf do} \\ {\bf x} := {\bf x} - 1 \\ {\bf else} \\ {\bf y} := {\bf x} + 2 \\ {\bf end} \\ {\bf x} := {\bf x} - 1 \\ {\bf end} \\ {\bf x} := {\bf x} - 1 \end{array}
```

- (a) Draw the control flow graph of the program fragment.
- (b) Annotate the control flow graph with the analysis result of a reaching definitions analysis.
- (c) Provide the use-definition information for the program variables x and y.

2 Live variables analysis

Consider the following program fragment:

```
x := y

x := x - 1

x := 4

while y < x do

y := y + x

end

y := 0
```

- (a) Identify the elementary blocks of the program and label them.
- (b) Write down the data flow equations for a live variables analysis of the program.
- (c) Solve the data flow equations using chaotic iteration.
- (d) Using the result obtained in (c), perform dead code elimination of the program fragment.
- (e) After step (d), is the resulting program free of dead variables? If not, explain why and modify the live variables analysis so that it can be used to produce a program free of dead variables.