

Software Verification

Exercise: Slicing and Abstract Interpretation

1 Program slicing

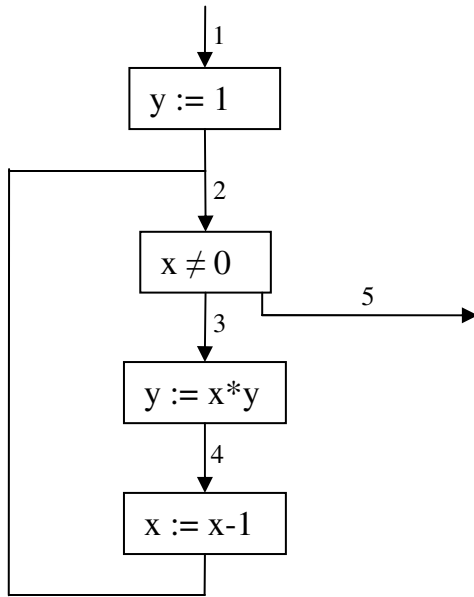
Consider the following program fragment:

```
x := 0
y := 0
i := n
j := n
while i > 0 do
    x := x + 1
    i := i - 1
    j := i
    while j > 0 do
        y := y + 1
        j := j - 1
    end
end
print(x)
print(y)
```

- Draw the program dependency graph of the program fragment.
- Compute the backward slice of the program fragment for the slicing criteria `print(x)` and `print(y)`.

2 Abstract interpretation

Consider again the factorial algorithm from the lecture with sign analysis equations:



$$\begin{aligned}
 A_1 &= [x \mapsto +, y \mapsto \top] \\
 A_2 &= A_1[y \mapsto +] \sqcup A_4[x \mapsto A_4(x) \ominus +] \\
 A_3 &= A_2 \\
 A_4 &= A_3[y \mapsto A_3(x) \otimes A_3(y)] \\
 A_5 &= A_2 \sqcap [x \mapsto 0, y \mapsto \top]
 \end{aligned}$$

- (a) Compute the analysis result by chaotic iteration.
- (b) The analysis is rather imprecise. Improve the result of the analysis by:
1. Changing the program but not the analysis.
 2. Changing the analysis but not the program.