

Mock Exam 2

ETH Zurich

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Name: _____

Group: _____

Question 1	/ 10
Question 2	/ 14
Question 3	/ 16
Total	/ 40

1 Multiple choice (10 points)

Put checkmarks in the checkboxes corresponding to the correct statements. There is at least one correct answer per question. A correctly checked or unchecked box is worth 0.5 points. An incorrectly checked or unchecked box is worth 0 points. Completely unanswered questions are worth 0 points.

Example:

Which of the following statements are true?

- | | | |
|--|-------------------------------------|------------|
| a. The sun is a mass of incandescent gas. | <input checked="" type="checkbox"/> | 0.5 points |
| b. $2 \times 4 = 8$ | <input type="checkbox"/> | 0 points |
| c. "Rösti" is a kind of sausage. | <input checked="" type="checkbox"/> | 0 points |
| c. C is an object-oriented programming language. | <input type="checkbox"/> | 0.5 points |
-

Solution

- Data structures.
 - Hashtables map keys to values.
 - Arrays provide constant-time ($O(1)$) access in the worst case.
 - Hashtables are commonly implemented using binary search trees.
 - Every node in a linked list stores a reference to the next node, if it exists.
 - Binary trees provide $O(\log n)$ time access in the worst case.
- Inheritance and polymorphism.
 - In Eiffel, some classes do not share a common ancestor.
 - If class B inherits from class A , all of A 's features are available to it.
 - It is impossible to inherit from two classes directly.
 - Depending on the dynamic type of x , two calls to $x.f$ may execute different instructions.
 - If class B inherits from class A , then type A conforms to type B .
- Objects and classes
 - All types are either reference or expanded.
 - If an object is of an expanded type, its fields cannot be modified at runtime.
 - Suppliers of class C can use all the features of class C .
 - A class can be both a supplier and a client.
 - If C is a deferred class, then no entity can exist in a program with static type C .
- Design by Contract
 - An empty postcondition is equivalent to the postcondition **True**.
 - An empty precondition is equivalent to the precondition **False**.
 - When reasoning about a creation procedure *make*, you are allowed to assume that the class invariant of the object being created holds at the beginning of *make*.
 - The invariant of a descendant class implies the invariant of its ancestor.
 - A (non-creation) procedure with an empty contract and an empty body is correct.

2 Quadratic Contracts (14 points)

As you probably remember from the school math course, a *quadratic equation* is an equation of the form

$$ax^2 + bx + c = 0,$$

where x is a variable, $a, b, c \in \mathbb{R}$ are the *coefficients*, with $a \neq 0$.

The standard way of solving a quadratic equation is to first calculate its *discriminant* Δ . If $\Delta > 0$ the equation has two real solutions, if $\Delta = 0$ — a single real solution and if $\Delta < 0$ — no real solutions.

2.1 Your Task

Below you will find a skeleton of a class that stores and solves quadratic equations (uninteresting routine bodies are omitted). The class also contains mathematical functions that are useful in the specification and/or implementation of the main features. Your task is to fill in the contracts (preconditions, postconditions and class invariants) according to the description given above and the header comments of the features. Note that the number of dotted lines does **not** indicate the number of contract clauses you have to provide.

You can use the following operations on real numbers: $+$, $-$, $*$, $/$, $>$, \geq , $<$, \leq . Do not use precise equality ($=$), as it produces unexpected results on machine floating point numbers. Instead use the function `approx(x, y: REAL): BOOLEAN` defined below, which determines whether two real numbers are equal with finite precision ε (in other words $|x - y| < \varepsilon$).

```
class
  QUADRATIC_EQUATION

create
  make

feature {NONE} -- Initialization
  make (coef_a, coef_b, coef_c: REAL)
    -- Create an equation with coefficients 'coef_a', 'coef_b', and 'coef_c'.
    -- Do not solve the equation yet.
  require
    coef_a_nonzero: not approx (coef_a, 0.0)
  do
    ...
  ensure
    a_set: approx (a, coef_a)
    b_set: approx (b, coef_b)
    c_set: approx (c, coef_c)
    no_solutions_yet: solution_count = 0
  end

feature -- Coefficients
  a, b, c: REAL
    -- Quadratic, linear and constant coefficients.

feature -- Math
  abs (x: REAL): REAL
    -- Absolute value of 'x'.
  do
```

```
...
ensure
  correct_result_positive :  $x \geq 0.0$  implies approx (Result, x)
  correct_result_negative :  $x < 0.0$  implies approx (Result, -x)
end

approx (x, y: REAL): BOOLEAN
  -- Is 'x' equal to 'y' with precision 'epsilon'?
do
  ...
ensure
  correct_result : Result = (abs (x - y) < epsilon)
end

epsilon: REAL = 1.e-10
  -- Precision with which reals are compared.

sqrt (x: REAL): REAL
  -- Square root of 'x'.
require
  x_non_negative:  $x \geq 0.0$ 
do
  ...
ensure
  correct_square : approx (Result * Result, x)
end

feature -- Solutions
  solution_count: INTEGER
    -- Number of solutions.

  solution (i: INTEGER): REAL
    -- Solution number 'i'.
  require
    i_not_too_small:  $i \geq 1$ 
    i_not_too_large :  $i \leq \text{solution\_count}$ 
  do
    if i = 1 then
      Result := x_1
    else
      Result := x_2
    end
  ensure
    is_solution : approx (a * Result * Result + b * Result + c, 0.0)
  end

feature -- Basic operations
  solve
    -- Solve the equation and store correct number of solutions in 'solution_count'.
  local
    d: REAL
  do
```

```
d := delta
if approx (d, 0) then
  solution_count := 1
  x_1 := - b / (2 * a)
elseif d > 0 then
  solution_count := 2
  x_1 := (-b + sqrt (d)) / (2 * a)
  x_2 := (-b - sqrt (d)) / (2 * a)
end
ensure
  not approx (delta, 0.0) and delta < 0.0 implies solution_count = 0
  approx (delta, 0.0) implies solution_count = 1
  not approx (delta, 0.0) and delta > 0.0 implies solution_count = 2
end

delta: REAL
  -- Discriminant of the equation.
do
  ...
end

feature {NONE} -- Implementation
  x_1, x_2: REAL
  -- Solutions.

invariant
  a_nonzero: not approx (a, 0.0)
end
```

3 Recursion: Deleting directories (16 Points)

In this question you will work with the *FILE* class, which represents both directories and regular files. You can iterate through the files contained in a directory using an internal cursor:

```
from
    directory . start
until
    directory . after
loop
    -- Do something with 'directory.item'
    directory . forth
end
```

The *delete* command of class *FILE* physically deletes the file from disk and changes the value of the *exists* query on the corresponding *FILE* object to **False**. For a directory this command only works if the directory is physically empty (i.e. no files physically exist in the directory).

3.1 Task 1

Take a look at the following procedure *delete_all*. It deletes a given directory with all its content using recursion:

```
delete_all ( directory: FILE)
2   require
    directory /= Void and then (directory.exists and directory.is_directory)
4   do
    from
6       directory . start
    until
8       directory . after
    loop
10      if directory.item.is_directory then
        delete_all (directory.item)
12      else -- regular file
        directory.item.delete
14      end
        directory . forth
16    end
        directory . delete
18  ensure
    not directory.exists
20  end
```

Your task is to rewrite *delete_all* so that it does not use recursion (the procedure is not allowed to call itself). You are not allowed to add new features. You are only allowed to call those features of class *FILE* that are already used in the recursive implementation of *delete_all*.

You can use the class *LIST* for this task. An excerpt is given at the end of the question.

Solution

Version 1

```
delete_all ( directory: FILE)
```

```
2  require
   directory /= Void and then (directory.exists and directory.is_directory)
4  local
   directories : LIST [FILE]
6  cur_directory : FILE
   do
8  -- delete all files
   from
10  create directories
   directories . extend_back ( directory )
12  directories . start
   until
14  directories . after
   loop
16  cur_directory := directories . item
   from
18  cur_directory . start
   until
20  cur_directory . after
   loop
22  if cur_directory . item . is_directory then
   directories . extend_back ( cur_directory . item )
24  else -- normal file
   cur_directory . item . delete
26  end
   cur_directory . forth
28  end
   directories . forth
30  end
   -- delete all directories
32  from
   directories . finish
34  until
   directories . before
36  loop
   directories . item . delete
38  directories . back
   end
40  ensure
   not directory . exists
42  end
```

Version 2

```
delete_all ( directory : FILE )
2  require
   directory /= Void and then (directory.exists and directory.is_directory)
4  local
   directories : LIST [FILE]
6  cur_directory : FILE
   do
8  from
```

```

10     create directories
11         directories .extend_back ( directory)
12     until
13         directories .is_empty
14     loop
15         cur_directory := directories .last
16         directories .remove_back
17
18     from
19         cur_directory .start
20     until
21         cur_directory .after
22     loop
23         if cur_directory .item .is_directory then
24             -- Save the current directory and restart the loop
25             -- with the subdirectory as 'cur_directory'
26             directories .extend_back ( cur_directory)
27             cur_directory := cur_directory .item
28             cur_directory .start
29         else -- normal file
30             cur_directory .item .delete
31             cur_directory .forth
32         end
33     end
34
35     cur_directory .delete
36 end
37 ensure
38     not directory .exists
39 end
    
```

3.2 Task 2

With the following example directory and the invocation

```
delete_all (create {FILE}.make ("C:\Temp\to_del"))
```

please give the order in which the files will be deleted for (a) the given recursive algorithm and (b) your non-recursive algorithm (e.g.: 3, 6, 7, 8, 9, 2, 5, 4, 1).

```

1 C:\Temp\to_del
2 C:\Temp\to_del\1
3 C:\Temp\to_del\1\foo.txt
4 C:\Temp\to_del\2
5 C:\Temp\to_del\2\3
6 C:\Temp\to_del\2\3\foobar.txt
7 C:\Temp\to_del\2\bar.txt
8 C:\Temp\to_del\another_file.txt
9 C:\Temp\to_del\file.txt
    
```

Solution

- a) 3, 2, 6, 5, 7, 4, 8, 9, 1
- b) 8, 9, 3, 7, 6, 5, 4, 2, 1

3.3 LIST [G] (Excerpt)

```
class LIST [G]

feature -- Access
  first : like item
    -- Item at first position

  item: G
    -- Current item

  last : like item
    -- Item at last position

feature -- Status report
  after: BOOLEAN
    -- Is there no valid cursor position to the right of cursor?

  before: BOOLEAN
    -- Is there no valid cursor position to the left of cursor?

  is_empty: BOOLEAN
    -- Is the list empty?

feature -- Cursor movement
  back
    -- Move to previous item.

  finish
    -- Move cursor to last position. (Go before if empty.)

  forth
    -- Move cursor to next position.

  start
    -- Move cursor to first position. (Go after if empty.)

feature -- Element change
  extend_back (v: like item)
    -- Add 'v' to end. Do not move cursor.

  extend_front (v: like item)
    -- Add 'v' to beginning. Do not move cursor.

  remove_back
    -- Remove last item. Move cursor after if on last.

  remove_front
    -- Remove first item. Move cursor before if on first .

end -- class LIST
```