

REACHABILITY ANALYSIS OF PROGRAM VARIABLES

Đurica Nikolić

ETH - Chair of Software Engineering

November 6th, 2013



STATIC ANALYSIS - BASIC FACTS

- PROVIDES FACTS ABOUT **RUN-TIME BEHAVIOR** OF PROGRAMS **BEFORE THEIR EXECUTIONS**:
 - NO DIVISION BY ZERO
 - NO NULL DEREFERENCE
 - NO INFINITE LOOPS
 - ...
- NUMERICAL PROPERTIES VS. **MEMORY-RELATED PROPERTIES**
- **OVER-APPROXIMATIONS** VS. **UNDER-APPROXIMATIONS**
- **ABSTRACT INTERPRETATION** [**CousotCousot77**] USUALLY HELPS

STATIC ANALYSIS - MAIN ISSUES

STATIC ANALYSIS OF REAL LIFE SOFTWARE IS EXTREMELY DIFFICULT:

- **COMPLEX SEMANTICS** OF CURRENT PROGRAMMING LANGUAGES
- **MEMORY-RELATED PROPERTIES** REQUIRED
- **SIDE-EFFECTS** OF METHOD CALLS
- **EXCEPTIONAL BEHAVIORS** SHOULD BE HANDLED
- **LIBRARIES** HEAVILY USED
- **ANNOTATIONS** HELP, BUT...
- **FORMALIZATION** VS. **IMPLEMENTATION**
- PROOF OF **SOUNDNESS** IS **DIFFICULT**

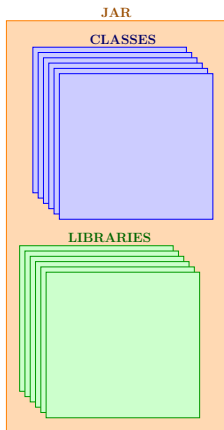
STATIC ANALYSIS - MAIN ISSUES

STATIC ANALYSIS OF REAL LIFE SOFTWARE IS EXTREMELY DIFFICULT:

- **COMPLEX SEMANTICS** OF CURRENT PROGRAMMING LANGUAGES
- **MEMORY-RELATED PROPERTIES** REQUIRED
- **SIDE-EFFECTS** OF METHOD CALLS
- **EXCEPTIONAL BEHAVIORS** SHOULD BE HANDLED
- **LIBRARIES** HEAVILY USED
- **ANNOTATIONS** HELP, BUT...
- **FORMALIZATION** VS. **IMPLEMENTATION**
- PROOF OF **SOUNDNESS** IS **DIFFICULT**

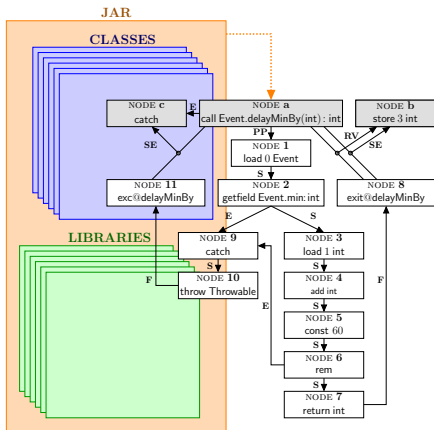
A GENERIC FRAMEWORK FOR CONSTRAINT-BASED STATIC ANALYSES OF JAVA BYTECODE PROGRAMS [NikolicPhD] DEALS WITH ALL THESE ISSUES.

FIRST STEPS



● JAR: CLASSES AND LIBRARIES

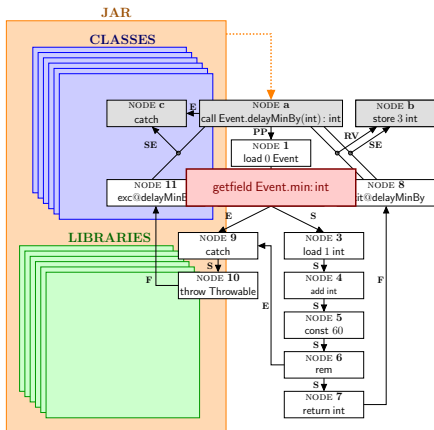
FIRST STEPS



● **JAR**: CLASSES AND LIBRARIES

● **CFG**: EXTRACTED FROM **JAR**

FIRST STEPS

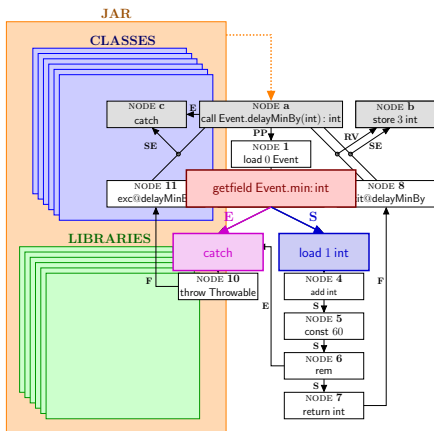


● JAR: CLASSES AND LIBRARIES

● CFG: EXTRACTED FROM JAR

● NODES

FIRST STEPS



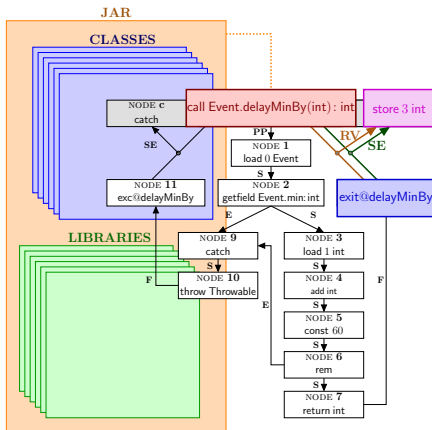
- **JAR**: CLASSES AND LIBRARIES

- **CFG**: EXTRACTED FROM JAR

- **NODES**

- **SEQUENTIAL** AND **EXCEPTIONAL** ARCS

FIRST STEPS



- JAR: CLASSES AND LIBRARIES

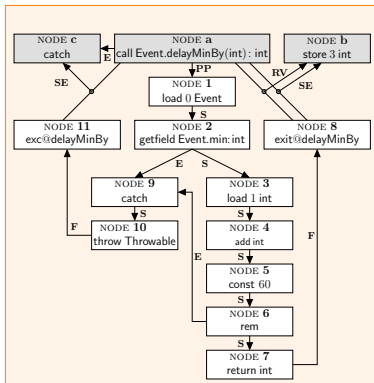
- CFG: EXTRACTED FROM JAR

- NODES

- SEQUENTIAL AND EXCEPTIONAL ARCS

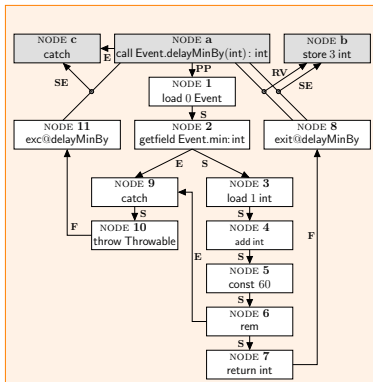
- RETURN VALUE AND SIDE-EFFECTS ARCS

ABSTRACT CONSTRAINT GRAPHS



ABSTRACT CONSTRAINT GRAPHS

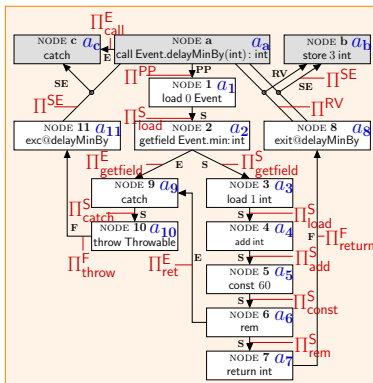
\mathcal{A} - GENERIC ABSTRACT DOMAIN



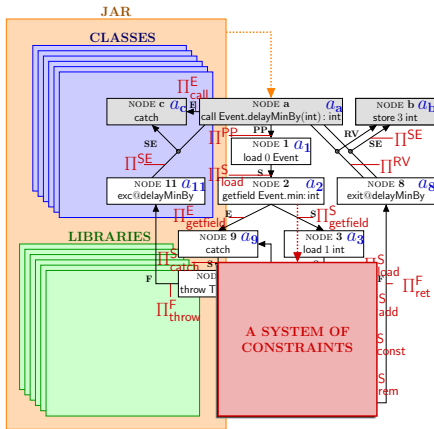
ABSTRACT CONSTRAINT GRAPHS

\mathcal{A} - GENERIC ABSTRACT DOMAIN

$\Pi_{ins} : \mathcal{A} \rightarrow \mathcal{A}$ - GENERIC PROPAGATION RULE (ABSTRACT SEMANTICS OF ins)

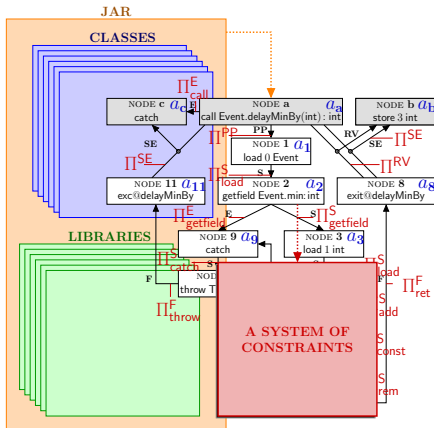


FROM ACG TO CONSTRAINT-BASED STATIC ANALYSES



- **JAR**: CLASSES AND LIBRARIES
- **CFG**: EXTRACTED FROM **JAR**
 - **NODES**
 - **SEQUENTIAL AND EXCEPTIONAL ARCS**
 - **RETURN VALUE AND SIDE-EFFECTS ARCS**
- **ABSTRACT CONSTRAINTS GRAPH**
- **A SYSTEM OF CONSTRAINTS - STATIC ANALYSIS**

FROM ACG TO CONSTRAINT-BASED STATIC ANALYSES



- **JAR**: CLASSES AND LIBRARIES
- **CFG**: EXTRACTED FROM **JAR**
 - **NODES**
 - **SEQUENTIAL AND EXCEPTIONAL ARCS**
 - **RETURN VALUE AND SIDE-EFFECTS ARCS**
- **ABSTRACT CONSTRAINTS GRAPH**
- **A SYSTEM OF CONSTRAINTS - STATIC ANALYSIS**
- **REQUIREMENTS!!!**

\mathcal{A} SATISFIES ACC, EACH Π_{ins} MONOTONIC, EACH Π_{ins} SOUNDLY APPROXIMATES ins
 \Rightarrow **SOUNDNESS!!!**

USER VS. FRAMEWORK

USER	FRAMEWORK
<ul style="list-style-type: none">• INSTANTIATE \mathcal{A} (PROPERTY)• INSTANTIATE Π_{ins} FOR EACH ins (ABSTRACT SEMANTICS OF ins)• SHOW THAT \mathcal{A} AND EACH Π_{ins} MEET FRAMEWORK'S REQUIREMENTS	<ul style="list-style-type: none">• EXTRACT CFG FROM A JAR• CONSTRUCT ACG USING Π_{ins}S• EXTRACT CONSTRAINTS FROM ACG• <u>EXISTENCE OF THE LEAST SOLUTION</u>• <u>SOUNDNESS OF THE SOLUTION</u>

JULIA - A STATIC ANALYZER FOR JAVA AND ANDROID



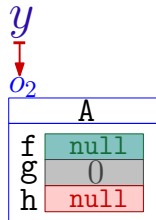
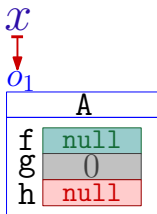
SEVERAL **CONSTRAINT-BASED STATIC ANALYSES** HAVE BEEN IMPLEMENTED INSIDE JULIA. THEY ARE USED LIKE **SUPPORTING ANALYSES** FOR JULIA'S **NULLNESS** AND **TERMINATION** TOOLS AND **IMPROVE** THEIR **PRECISION**. WWW.JULIASOFT.COM

- **DEFINITE ALIASING ANALYSIS**
- **POSSIBLE SHARING ANALYSIS** [SAS 2008]
- **POSSIBLE SIDE EFFECTS ANALYSIS**
- **POSSIBLE CREATION POINT ANALYSIS**
- **POSSIBLE REACHABILITY ANALYSIS** [IJCAR 2012, TOPLAS 2013]
- **DEFINITE EXPRESSION ALIASING ANALYSIS** [ICTAC 2012]

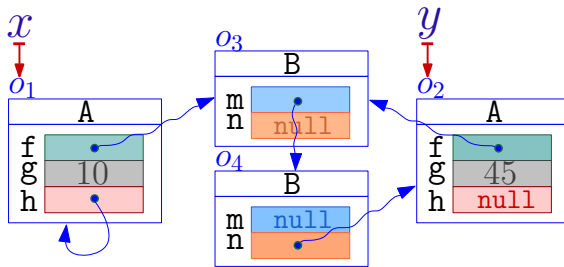
REACHABILITY ANALYSIS OF VARIABLES: AN EXAMPLE OF CONSTRAINT-BASED STATIC ANALYSIS

[IJCAR 2012, TOPLAS 2013]

INTUITIVE DEFINITION OF REACHABILITY

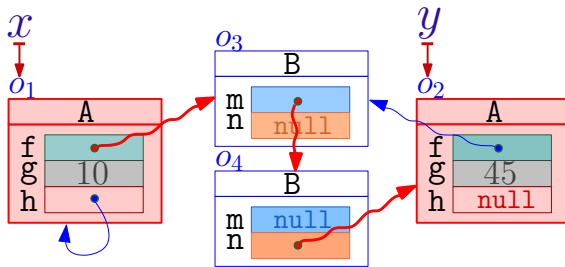


INTUITIVE DEFINITION OF REACHABILITY



Is there a sequence of fields f_1, \dots, f_k such that $x.f_1 \dots f_k = y$?

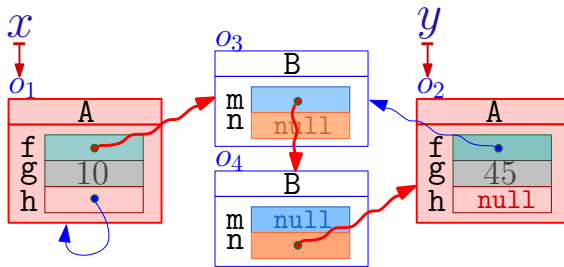
INTUITIVE DEFINITION OF REACHABILITY



IS THERE A SEQUENCE OF FIELDS f_1, \dots, f_k SUCH THAT $x.f_1 \dots f_k = y$?

$x.f.m.n = y$

INTUITIVE DEFINITION OF REACHABILITY



Is there a sequence of fields f_1, \dots, f_k such that $x.f_1 \dots f_k = y$?

$x.f.m.n = y \Rightarrow x \text{ REACHES } y$

A SIMPLE EXAMPLE - LIST OF STUDENTS

```
public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public static void main(String[] args) {
        List<Student> list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>();
            tmp.head = student;
            tmp.tail = list;
            list = tmp;
        }
    }
}
```

A SIMPLE EXAMPLE - LIST OF STUDENTS

```
public class Student {  
    String name;  
    ...  
}  
  
public class List<Student> {  
    public Student head;  
    public List<Student> tail;  
  
    public static void main(String[] args) {  
        List<Student> list = null;  
        for (int i = 1; i <= n; i++) {  
            Student student = new Student(i);  
            List<Student> tmp = new List<Student>();  
            tmp.head = student;  
            tmp.tail = list;  
            list = tmp;  
        }  
    }  
}
```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b

A SIMPLE EXAMPLE - LIST OF STUDENTS

```

public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public static void main(String[] args) {
        List<Student> list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>();
            tmp.head = student;
            tmp.tail = list;
            list = tmp;
        }
    }
}

```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b
 $\text{tmp} \rightsquigarrow \text{student}$

A SIMPLE EXAMPLE - LIST OF STUDENTS

```

public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public static void main(String[] args) {
        List<Student> list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>();
            tmp.head = student;
            tmp.tail = list;
            list = tmp;
        }
    }
}

```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b

tmp	\rightsquigarrow	student
list	\rightsquigarrow	tmp

A SIMPLE EXAMPLE - LIST OF STUDENTS

```

public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public static void main(String[] args) {
        List<Student> list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>();
            tmp.head = student;
            tmp.tail = list;
            list = tmp;
        }
    }
}

```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b

tmp \rightsquigarrow student

list \rightsquigarrow tmp

list \rightsquigarrow student

A SIMPLE EXAMPLE 2 - LIST OF STUDENTS

```
public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public List(Student head, List<Student> tail) {
        this.head = head;
        this.tail = tail;
    }

    public static void main(String[] args) {
        ListStudent list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>(student, list);
            list = tmp;
        }
    }
}
```

A SIMPLE EXAMPLE 2 - LIST OF STUDENTS

```
public class Student {  
    String name;  
    ...  
}  
  
public class List<Student> {  
    public Student head;  
    public List<Student> tail;  
  
    public List(Student head, List<Student> tail) {  
        this.head = head;  
        this.tail = tail;  
    }  
  
    public static void main(String[] args) {  
        ListStudent list = null;  
        for (int i = 1; i <= n; i++) {  
            Student student = new Student(i);  
            List<Student> tmp = new List<Student>(student, list);  
            list = tmp;  
        }  
    }  
}
```

REACHABILITY

a REACHES ***b***, i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO ***b***

A SIMPLE EXAMPLE 2 - LIST OF STUDENTS

```

public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public List(Student head, List<Student> tail) {
        this.head = head;
        this.tail = tail;
    }

    public static void main(String[] args) {
        ListStudent list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>(student, list);
            list = tmp;
        }
    }
}

```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b

tmp \rightsquigarrow student

tmp \rightsquigarrow list

A SIMPLE EXAMPLE 2 - LIST OF STUDENTS

```

public class Student {
    String name;
    ...
}

public class List<Student> {
    public Student head;
    public List<Student> tail;

    public List(Student head, List<Student> tail) {
        this.head = head;
        this.tail = tail;
    }

    public static void main(String[] args) {
        ListStudent list = null;
        for (int i = 1; i <= n; i++) {
            Student student = new Student(i);
            List<Student> tmp = new List<Student>(student, list);
            list = tmp;
        }
    }
}

```

REACHABILITY

a REACHES b , i.e., $a \rightsquigarrow b$ iff

a REACHES A LOCATION BOUND TO b
 $\text{tmp} \rightsquigarrow \text{student}$

$\text{list} \rightsquigarrow \text{student}$

$\text{list} \rightsquigarrow \text{tmp}$

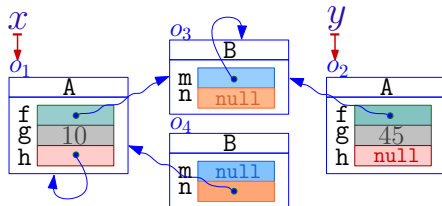
HAVEN'T WE SOLVED THIS PROBLEM YET?

THERE IS A LOT OF POINTER ANALYSES: [HIND01] SURVEYS MORE THAN 75 PAPERS

HAVEN'T WE SOLVED THIS PROBLEM YET?

THERE IS A LOT OF POINTER ANALYSES: [Hind01] SURVEYS MORE THAN 75 PAPERS

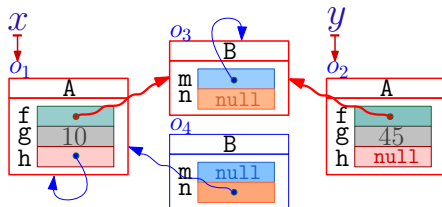
● SHARING ANALYSIS



HAVEN'T WE SOLVED THIS PROBLEM YET?

THERE IS A LOT OF POINTER ANALYSES: [Hind01] SURVEYS MORE THAN 75 PAPERS

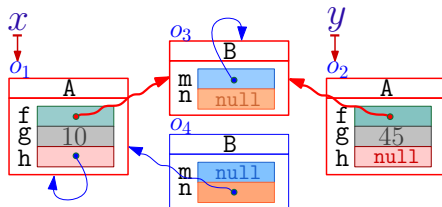
● SHARING ANALYSIS



HAVEN'T WE SOLVED THIS PROBLEM YET?

THERE IS A LOT OF POINTER ANALYSES: [Hind01] SURVEYS MORE THAN 75 PAPERS

- SHARING ANALYSIS

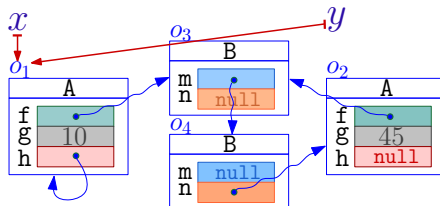


- REACHABILITY ~~ENTAILS~~ SHARING
- SHARING ~~ENTAILS~~ REACHABILITY

HAVEN'T WE SOLVED THIS PROBLEM YET?

THERE IS A LOT OF POINTER ANALYSES: [Hind01] SURVEYS MORE THAN 75 PAPERS

- SHARING ANALYSIS
- ALIASING ANALYSIS



- ALIASING ~~ENTAILS~~ REACHABILITY
- REACHABILITY ~~ENTAILS~~ ALIASING

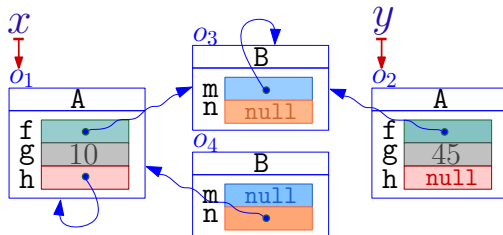
WHERE CAN IT BE USEFUL?

CYCLICITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

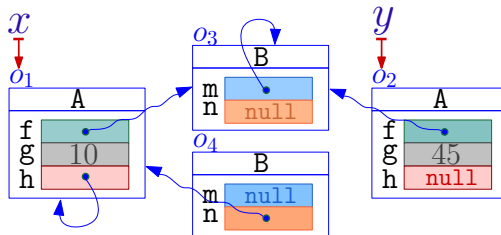
"SHARING" APPROACH



WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"SHARING" APPROACH

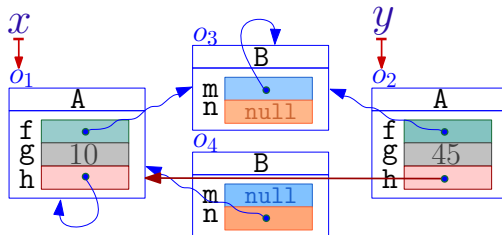


$y.h = x$ MAKES y CYCLICAL?

WHERE CAN IT BE USEFUL?

CYCLICITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"SHARING" APPROACH

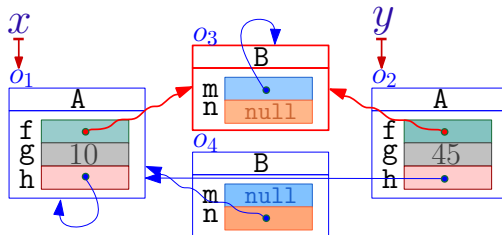


$y.h = x$ MAKES y CYCLICAL?

WHERE CAN IT BE USEFUL?

CYCLICITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"SHARING" APPROACH

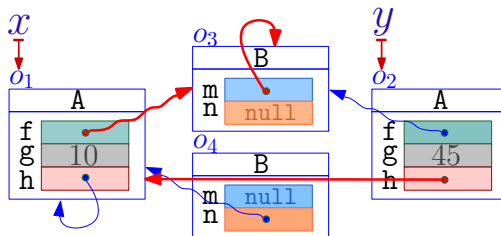


$y.h = x$ MAKES y CYCLICAL?
IF x SHARES WITH y ?

WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"SHARING" APPROACH

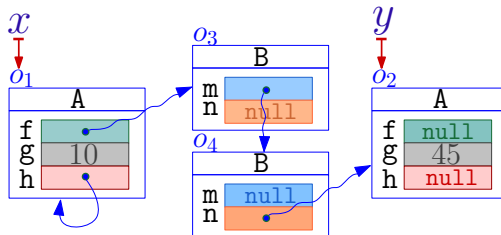


$y.h = x$ MAKES y CYCLICAL? **No!**

WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

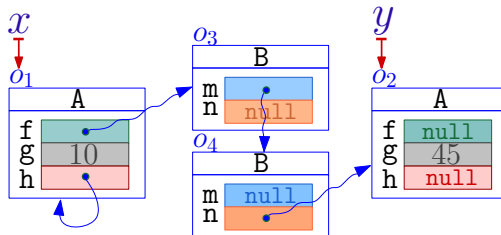
"REACHABILITY" APPROACH



WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"REACHABILITY" APPROACH

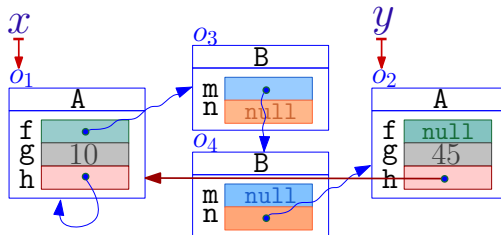


$y.h = x$ MAKES y CYCLICAL?

WHERE CAN IT BE USEFUL?

CYCLICITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

"REACHABILITY" APPROACH

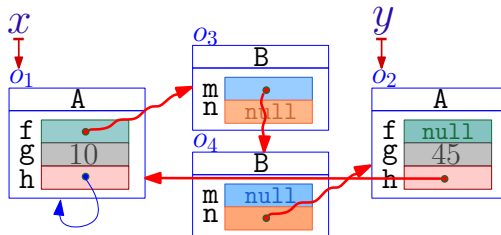


$y.h = x$ MAKES y CYCLICAL?
IF x REACHES y

WHERE CAN IT BE USEFUL?

CYCLOCITY ANALYSIS: AN ASSIGNMENT $y.h = x$ MIGHT MAKE y CYCLICAL?

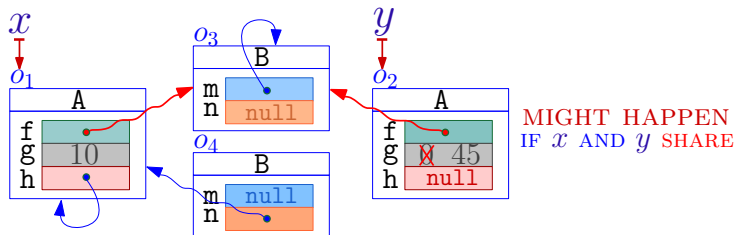
"REACHABILITY" APPROACH



$y.h = x$ MAKES y CYCLICAL? **YES!**

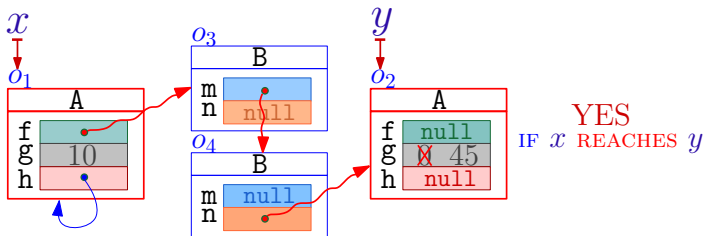
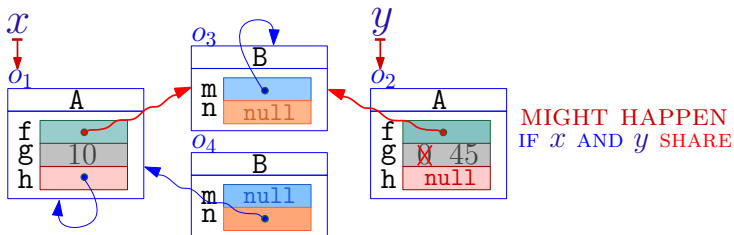
WHERE CAN IT BE USEFUL?

SIDE-EFFECTS ANALYSIS: AN ASSIGNMENT $y.g = 45$ MIGHT AFFECT A PARAMETER x OF A METHOD m ?



WHERE CAN IT BE USEFUL?

SIDE-EFFECTS ANALYSIS: AN ASSIGNMENT $y.g = 45$ MIGHT AFFECT A PARAMETER x OF A METHOD m ?



TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```
const v  
dup t  
load k t  
store k t  
ifne t  
new  $\kappa$   
getfield  $\kappa.f:t$   
putfield  $\kappa.f:t$   
throw  $\kappa$   
catch  
exception_is K
```


TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```
const v
dup t
load k t    BASIC INSTRUCTIONS
store k t
ifne t
new  $\kappa$ 
getfield  $\kappa.f:t$ 
putfield  $\kappa.f:t$ 
throw  $\kappa$ 
catch
exception_is K
```

TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```
const v
dup t
load k t
store k t
ifne t
new  $\kappa$ 
getfield  $\kappa.f:t$       OBJECT-MANIPULATING
putfield  $\kappa.f:t$ 
throw  $\kappa$ 
catch
exception_is K
```

TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```
const v
dup t
load k t
store k t
ifne t
new  $\kappa$ 
getfield  $\kappa.f:t$ 
putfield  $\kappa.f:t$ 
throw  $\kappa$ 
catch      EXCEPTION-HANDLING
exception_is  $K$ 
```

TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```
const v  
dup t  
load k t  
store k t  
ifne t  
new  $\kappa$   
getfield  $\kappa.f:t$   
putfield  $\kappa.f:t$   
throw  $\kappa$   
catch  
exception_is  $K$ 
```

OUR IMPLEMENTATION HANDLES ALL JAVA TYPES AND BYTECODES.

TARGET LANGUAGE: A FRAGMENT OF JAVA BYTECODE

```

...
tmp.tail = list;
...

    load 4 List
    load 1 List
    putfield List.tail: List

tmp    ↔ l4
list   ↔ l1

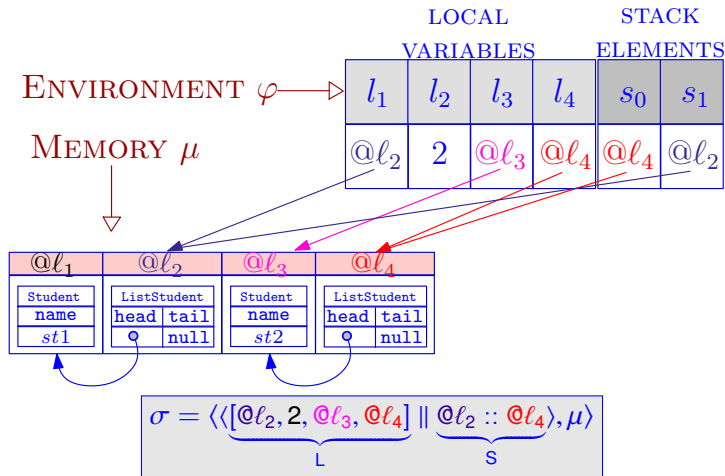
```

STATE

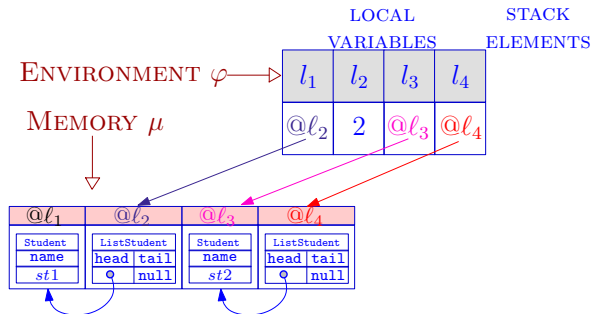
SOME DEFINITIONS:

- WE DISTINGUISH **LOCAL** ($L = \{l_0, l_1, \dots\}$) AND **STACK** ($S = \{s_0, s_1, \dots\}$) VARIABLES;
- VALUES CAN BE **INTEGERS** (\mathbb{Z}), **LOCATIONS** ($\mathbb{L} = \{@\ell_1, \dots\}$) AND **null**;
- **OBJECTS** CONTAIN FIELDS AND HAVE METHODS;
- **ENVIRONMENTS** MAP VARIABLES INTO VALUES $\varphi : L \cup S \rightarrow \mathbb{Z} \cup \mathbb{L} \cup \{\text{null}\}$;
- **MEMORIES** μ MAP LOCATIONS TO OBJECTS;
- **STATES** ARE TUPLES $\langle \varphi, \mu \rangle$;
- Σ DENOTES THE SET OF ALL POSSIBLE STATES.

STATE

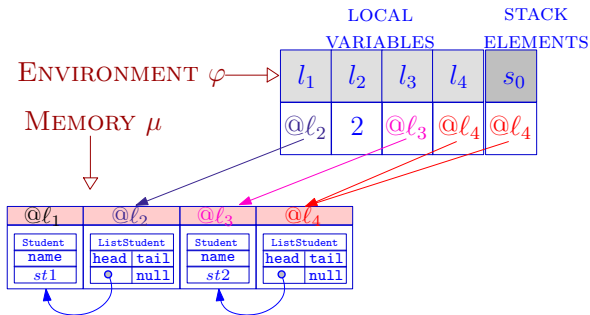


SEMANTICS OF `tmp.tail = list` AT BYTECODE LEVEL



```
load 4 List
load 1 List
putfield List.tail:List
```


SEMANTICS OF `tmp.tail = list` AT BYTECODE LEVEL

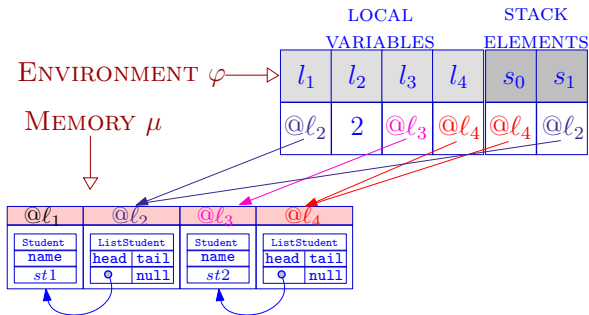


load 4 List

load 1 List

putfield List.tail:List

SEMANTICS OF `tmp.tail = list` AT BYTECODE LEVEL

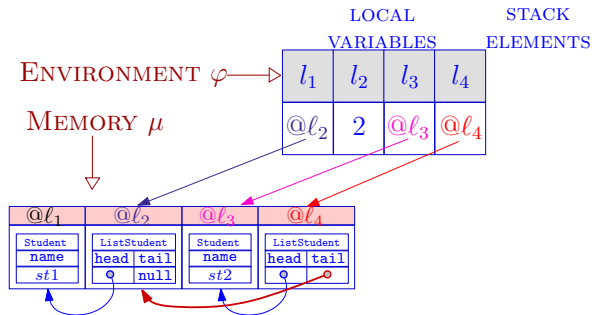


load 4 List

load 1 List

putfield List.tail:List

SEMANTICS OF `tmp.tail = list` AT BYTECODE LEVEL



load 4 List

load 1 List

putfield List.tail:List

REACHABLE LOCATIONS AND VARIABLES

REACHABLE LOCATIONS $L_\sigma(a)$

GIVEN A STATE $\sigma = \langle \varphi, \mu \rangle$ AND A LOCATION $@\ell$, LOCATIONS REACHABLE FROM $@\ell$ IN σ ARE $L_\sigma(@\ell) = \text{lfp}_{i \geq 0} L_\sigma^i(@\ell)$, WHERE $L_\sigma^i(@\ell)$ REPRESENTS THE SET OF LOCATIONS REACHABLE FROM $@\ell$ IN i STEPS, I.E.,

$$L_\sigma^i(@\ell) = \begin{cases} \{@\ell\} & \text{IF } i = 0 \\ \bigcup_{@\ell_1 \in L_\sigma^{i-1}(@\ell)} (\text{rng}(\mu(@\ell_1). \phi) \cap \mathbb{L}) \cup L_\sigma^{i-1}(@\ell) & \text{OTHERWISE.} \end{cases}$$

REACHABLE LOCATIONS AND VARIABLES

REACHABLE LOCATIONS $L_\sigma(a)$

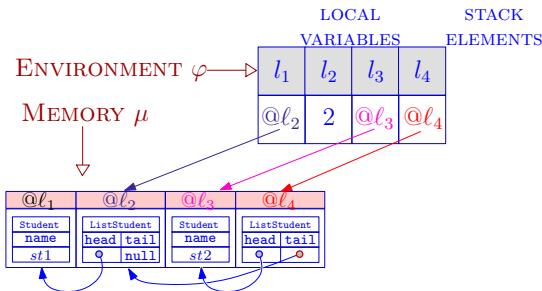
GIVEN A STATE $\sigma = \langle \varphi, \mu \rangle$ AND A LOCATION $@\ell$, LOCATIONS REACHABLE FROM $@\ell$ IN σ ARE $L_\sigma(@\ell) = \text{lfp}_{i \geq 0} L_\sigma^i(@\ell)$, WHERE $L_\sigma^i(@\ell)$ REPRESENTS THE SET OF LOCATIONS REACHABLE FROM $@\ell$ IN i STEPS, I.E.,

$$L_\sigma^i(@\ell) = \begin{cases} \{@\ell\} & \text{IF } i = 0 \\ \bigcup_{@\ell_1 \in L_\sigma^{i-1}(@\ell)} (\text{rng}(\mu(@\ell_1). \phi) \cap \mathbb{L}) \cup L_\sigma^{i-1}(@\ell) & \text{OTHERWISE.} \end{cases}$$

REACHABILITY OF VARIABLES $a \rightsquigarrow^\sigma b$

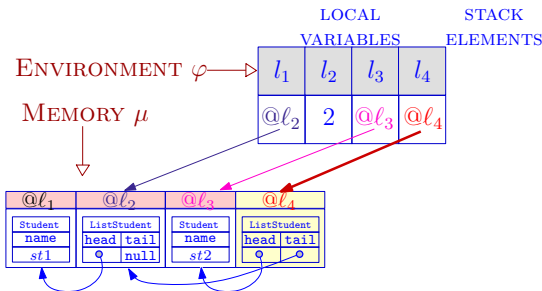
WE SAY THAT A VARIABLE b IS REACHABLE FROM A VARIABLE a IN σ , AND WE DENOTE IT $a \rightsquigarrow^\sigma b$ IFF $\varphi(a), \varphi(b) \in \mathbb{L}$ AND $\varphi(b) \in L_\sigma(a)$.

REACHABLE LOCATIONS AND VARIABLES



WHICH LOCATIONS ARE REACHABLE FROM $@l_4$?

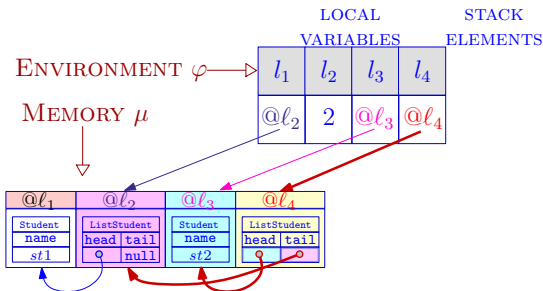
REACHABLE LOCATIONS AND VARIABLES



WHICH LOCATIONS ARE REACHABLE FROM $@l_4$?

$$L_o^0(@l_4) = \{ @l_4 \}$$

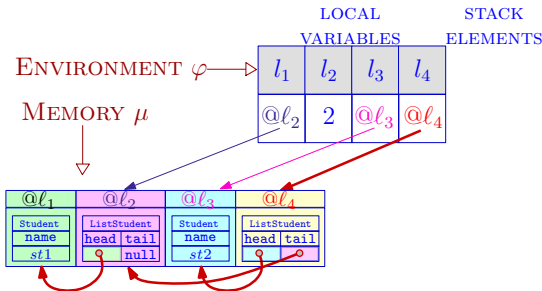
REACHABLE LOCATIONS AND VARIABLES



WHICH LOCATIONS ARE REACHABLE FROM $@l_4$?

$$\begin{aligned}
 L_{\sigma}^0(@l_4) &= \{ @l_4 \} \\
 L_{\sigma}^1(@l_4) &= \{ @l_2, @l_3, @l_4 \}
 \end{aligned}$$

REACHABLE LOCATIONS AND VARIABLES



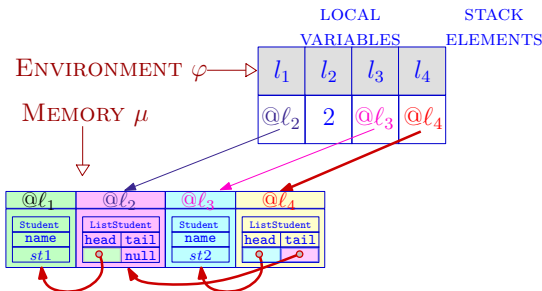
WHICH LOCATIONS ARE REACHABLE FROM $@l_4$?

$$L_{\sigma}^0(@l_4) = \{ @l_4 \}$$

$$L_{\sigma}^1(@l_4) = \{ @l_2, @l_3, @l_4 \}$$

$$L_{\sigma}^2(@l_4) = \{ @l_1, @l_2, @l_3, @l_4 \} \Rightarrow L_{\sigma}(@l_4) = \{ @l_1, @l_2, @l_3, @l_4 \}$$

REACHABLE LOCATIONS AND VARIABLES



WHICH LOCATIONS ARE REACHABLE FROM $@l_4$?

$$\begin{aligned}
 L_{\sigma}^0(@l_4) &= \{ @l_4 \} \\
 L_{\sigma}^1(@l_4) &= \{ @l_2, @l_3, @l_4 \} \\
 L_{\sigma}^2(@l_4) &= \{ @l_1, @l_2, @l_3, @l_4 \} \Rightarrow L_{\sigma}(@l_4) = \{ @l_1, @l_2, @l_3, @l_4 \}
 \end{aligned}$$

$$\varphi(l_4) = @l_4 \Rightarrow l_4 \rightsquigarrow^{\sigma} l_4$$

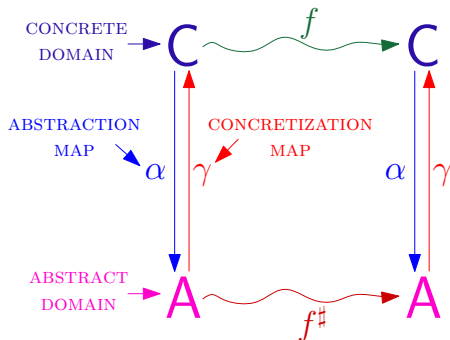
$$\varphi(l_1) = @l_2 \Rightarrow l_4 \rightsquigarrow^{\sigma} l_1$$

$$\varphi(l_3) = @l_3 \Rightarrow l_4 \rightsquigarrow^{\sigma} l_3$$

FORMAL DEFINITION DEPENDS ON THE CURRENT PROGRAM STATE, I.E.,
ON ONE PARTICULAR EXECUTION.

WE WANT TO DETERMINE AN APPROXIMATION OF THE REACHABILITY
HOLDING FOR ANY POSSIBLE EXECUTION.

ABSTRACT INTERPRETATION FRAMEWORK [CousotCousot77]



BEST CORRECT APPROXIMATION: $f^{bca} = \alpha \circ f \circ \gamma$

IN PRACTICE: f^\sharp IS LESS PRECISE THAN f^{bca} AND
INTRODUCES OVER-APPROXIMATION

CONCRETE AND ABSTRACT DOMAINS

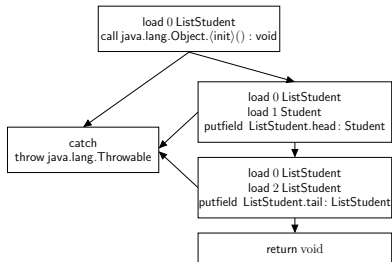
- Σ - SET OF ALL STATES
- V - SET OF ALL VARIABLES
- CONCRETE DOMAIN: $C = \langle \wp(\Sigma), \subseteq \rangle$
- ABSTRACT DOMAIN: $A = \langle \wp(V \times V), \subseteq \rangle$
 - AN ABSTRACT ELEMENT $R \in A$ REPRESENTS THOSE CONCRETE STATES WHOSE REACHABILITY INFORMATION IS OVER-APPROXIMATED BY THE PAIRS OF VARIABLES IN R
 - WE WRITE $a \rightsquigarrow b$ TO DENOTE $\langle a, b \rangle \in R$
- CONCRETIZATION MAP:

$$\gamma(R) = \{\sigma \in \Sigma \mid \forall a, b \in V. a \rightsquigarrow^\sigma b \Rightarrow a \rightsquigarrow b \in R\}$$

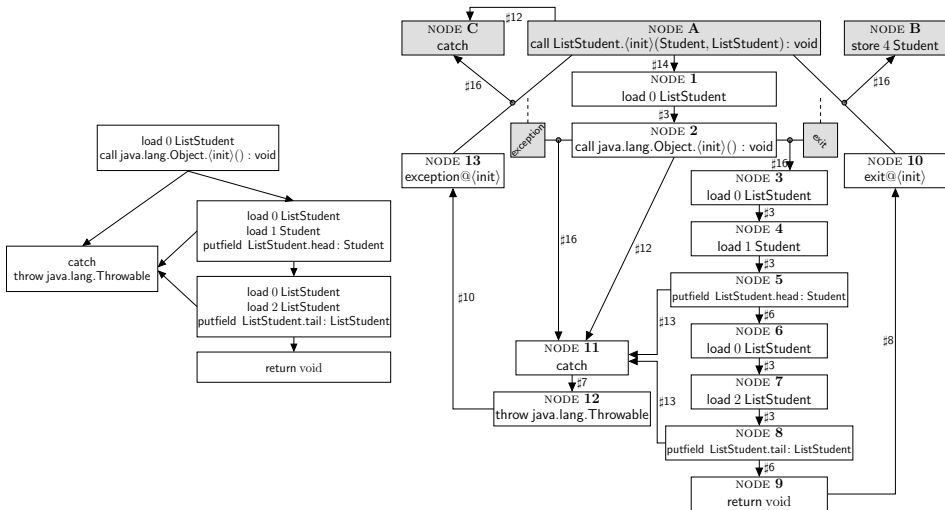
CONSTRAINT-BASED STATIC ANALYSIS - EXAMPLE

- **ABSTRACT CONSTRAINT GRAPH** ($ACG = \langle V, E \rangle$) GIVES RISE TO AN OVER-APPROXIMATION OF THE REACHABILITY INFORMATION AT EACH POINT OF A PROGRAM P .
- THE **CFG** OF P GIVES RISE TO THE NODES AND ARCS OF THE **ACG**, I.E., THERE IS A NODE FOR EVERY BYTECODE AND THERE IS AN ARC BETWEEN 2 NODES IF THEIR CORRESPONDING BYTECODES ARE ADJACENT IN THE **CFG**.
- **EACH NODE IS DECORATED BY AN ABSTRACT ELEMENT**, I.E., BY A SET OF ORDERED PAIRS OF VARIABLES REPRESENTING AN OVER-APPROXIMATION OF THE REACHABILITY INFORMATION AT THAT POINT.
- **ARCS PROPAGATE APPROXIMATIONS OF THE REACHABILITY OF THEIR SOURCES**, I.E., THEY REPRESENT **ABSTRACT SEMANTICS OF BYTECODES**.
- THE **REACHABILITY INFORMATION OF THE INITIAL NODE**, CORRESPONDING TO THE BEGINNING OF THE **MAIN METHOD** IS \emptyset , AND IT IS PROPAGATED THROUGH THE **ACG**.

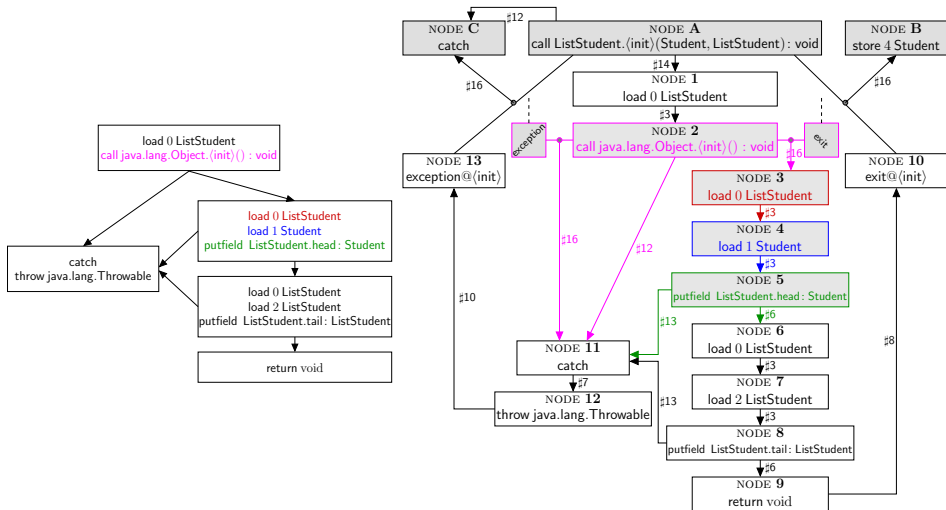
CONSTRAINT-BASED STATIC ANALYSIS - EXAMPLE



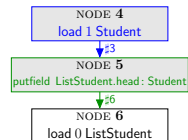
CONSTRAINT-BASED STATIC ANALYSIS - EXAMPLE



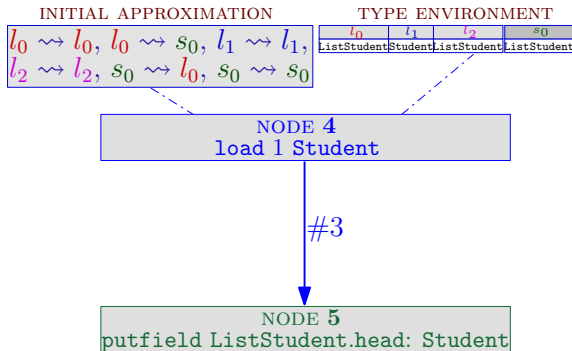
CONSTRAINT-BASED STATIC ANALYSIS - EXAMPLE



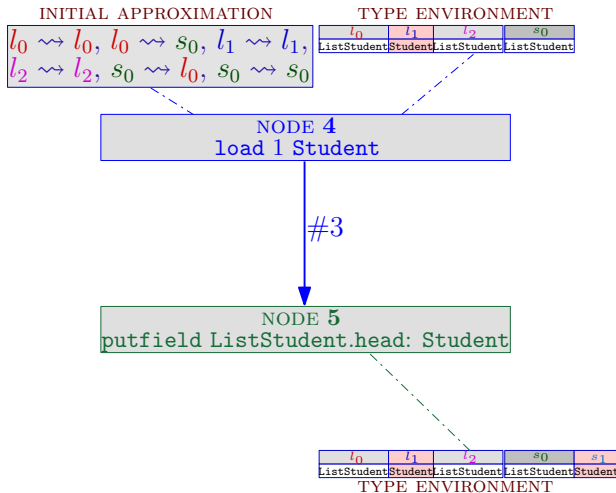
CONSTRAINT-BASED STATIC ANALYSIS - EXAMPLE



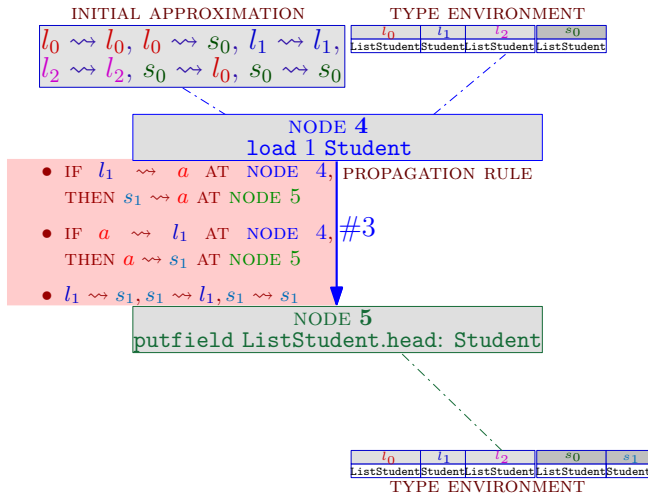
PROPAGATION RULES - EXAMPLE



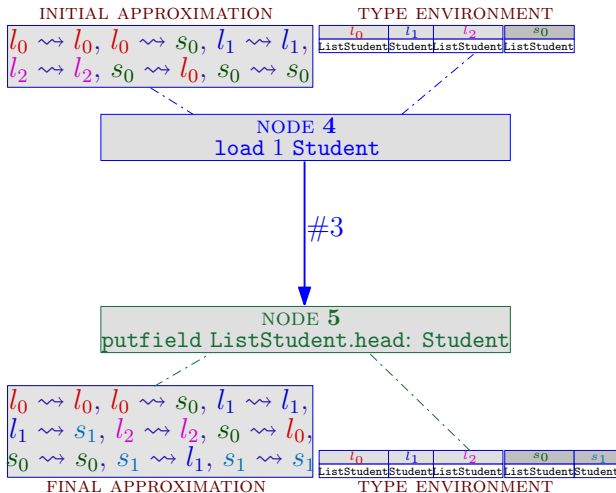
PROPAGATION RULES - EXAMPLE



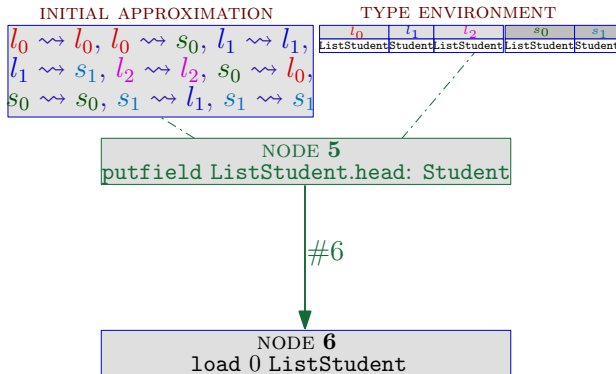
PROPAGATION RULES - EXAMPLE



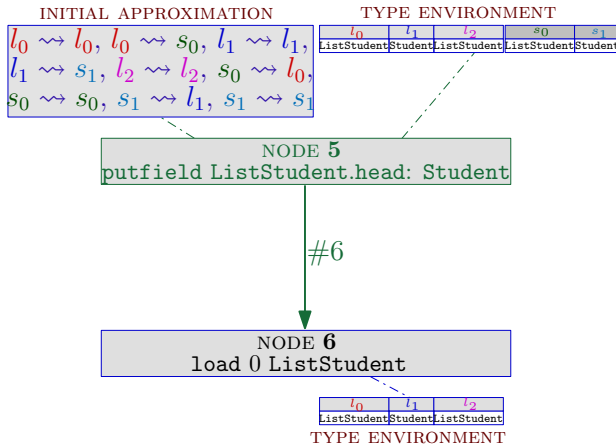
PROPAGATION RULES - EXAMPLE



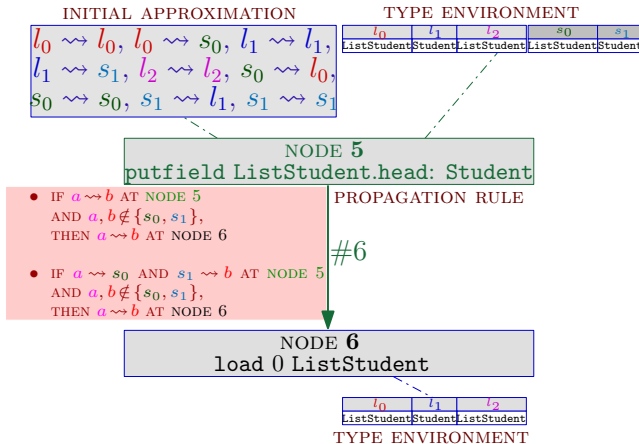
PROPAGATION RULES - EXAMPLE



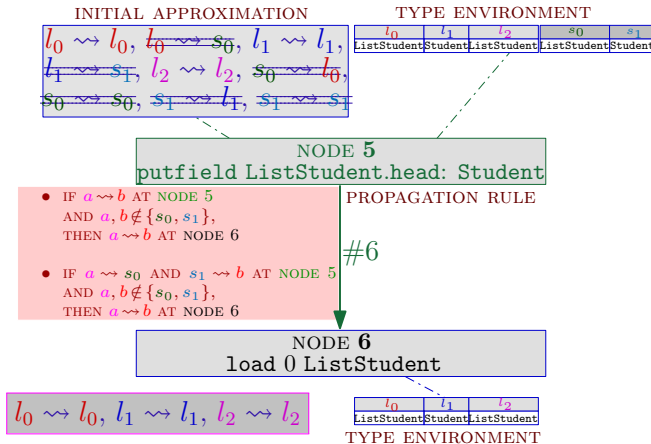
PROPAGATION RULES - EXAMPLE



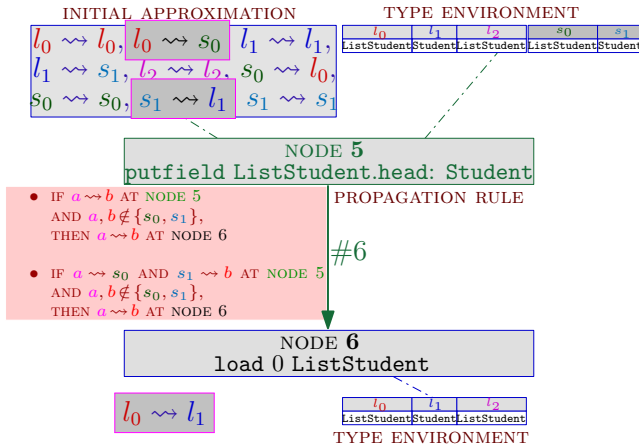
PROPAGATION RULES - EXAMPLE



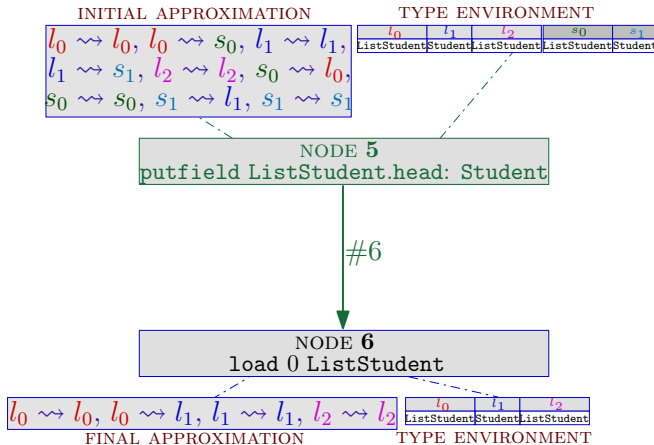
PROPAGATION RULES - EXAMPLE



PROPAGATION RULES - EXAMPLE



PROPAGATION RULES - EXAMPLE

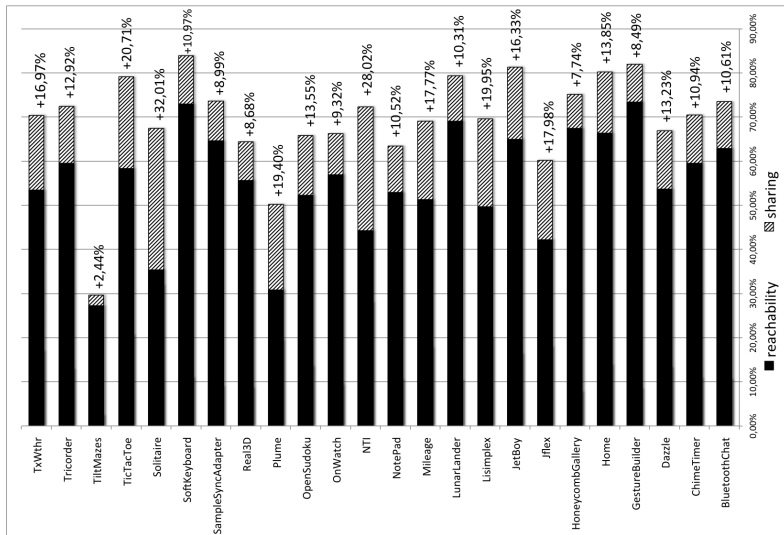


SOUNDNESS OF OUR APPROACH

LET ins AND $\sigma \in \Sigma$ BE A BYTECODE INSTRUCTION AND A STATE REACHED BY AN EXECUTION OF THE `main` METHOD OF A PROGRAM, AND LET $R_{ins} \in \mathcal{A}$ BE THE REACHABILITY APPROXIMATION COMPUTED BY OUR ANALYSIS AT ins . THEN,

$$\sigma \in \gamma(R_{ins}).$$

EXPERIMENTAL EVALUATION WITH JULIA - SHARING vs. REACHABILITY



Software verification made easy

your system multicore environment

EXPERIMENTAL EVALUATION WITH JULIA - IMPACT ON OTHER ANALYSES

REACHABILITY ANALYSIS	SIDE-EFFECTS ANALYSIS	FIELD INITIALIZAT. ANALYSIS

EXPERIMENTAL EVALUATION WITH JULIA - IMPACT ON OTHER ANALYSES

REACHABILITY ANALYSIS	SIDE-EFFECTS ANALYSIS	FIELD INITIALIZAT. ANALYSIS
45.07%		

the ratio of pairs of variables $\langle v, w \rangle$ such that the analysis concludes that v might reach w , over the total number of pairs of variables of reference type:
the lower the ratio, the higher the precision

EXPERIMENTAL EVALUATION WITH JULIA - IMPACT ON OTHER ANALYSES

REACHABILITY ANALYSIS	SIDE-EFFECTS ANALYSIS	FIELD INITIALIZAT. ANALYSIS
45.07%	-23.47%	

↓
which parameters p of a method might be affected
by its execution: the method might update a field of
an object reachable from p :
the lower the numbers, the better the precision

EXPERIMENTAL EVALUATION WITH JULIA - IMPACT ON OTHER ANALYSES

REACHABILITY ANALYSIS	SIDE-EFFECTS ANALYSIS	FIELD INITIALIZAT. ANALYSIS
45.07%	-23.47%	+3.46%

the number of fields of reference type proven to be always initialized before being read, in all constructors of their defining class:
the higher the numbers, the better the precision

EXPERIMENTAL EVALUATION WITH JULIA - IMPACT ON OTHER ANALYSES

REACHABILITY ANALYSIS	SIDE-EFFECTS ANALYSIS	FIELD INITIALIZAT. ANALYSIS
45.07%	-23.47%	+3.46%

	NULLNESS ANALYSIS	TERMINATION ANALYSIS
runtime	-7.77%	-1.62%
warnings	-3.38%	0%

STATIC ANALYSIS - MAIN ISSUES

STATIC ANALYSIS OF REAL LIFE SOFTWARE IS EXTREMELY DIFFICULT:

- **COMPLEX SEMANTICS** OF CURRENT PROGRAMMING LANGUAGES
- **MEMORY-RELATED PROPERTIES** REQUIRED
- **SIDE-EFFECTS** OF METHOD CALLS
- INSTRUCTIONS' **EXCEPTIONAL BEHAVIORS**
- **LIBRARIES** HEAVILY USED
- **ANNOTATIONS** HELP, BUT...
- **FORMALIZATION** VS. **IMPLEMENTATION**
- PROOF OF **SOUNDNESS** IS **DIFFICULT**

STATIC ANALYSIS - MAIN ISSUES

STATIC ANALYSIS OF REAL LIFE SOFTWARE IS EXTREMELY DIFFICULT:

- **COMPLEX SEMANTICS** OF CURRENT PROGRAMMING LANGUAGES **JAVA BYTECODE**
- **MEMORY-RELATED PROPERTIES** REQUIRED **REACHABILITY, SHARING, ALIASING, SIDE-EFFECTS**
- **SIDE-EFFECTS** OF METHOD CALLS **ACG'S SE ARCS DEAL WITH THEM**
- INSTRUCTIONS' **EXCEPTIONAL BEHAVIORS** **ACG'S EXCEPTIONAL ARCS DEAL WITH THEM**
- **LIBRARIES** HEAVILY USED **OUR CFG INCLUDES THEM**
- **ANNOTATIONS** HELP, BUT... **WE DO NOT USE ANNOTATIONS**
- **FORMALIZATION** VS. **IMPLEMENTATION** **DONE**
- **PROOF OF SOUNDNESS** IS **DIFFICULT** **OUR FRAMEWORK SIMPLIFIES THESE PROOFS**

QUESTIONS?