

# Mock Exam 2

ETH Zurich

December 3, 2014

Name: \_\_\_\_\_

Group: \_\_\_\_\_

Question 1	/ 13
Question 2	/ 10
Question 3	/ 13
Total	/ 36

## 1 Contracts (13 points)

We are interested in an adventure game in which knights wander through unknown lands. A knight owns coins that can be used for recruiting villagers as companions and for healing wounds. He also has a reputation ranging from -5 to 5, which is subtracted from the cost of recruiting and healing (see examples below). Even though the cost is reduced for the knights with good reputation, it can never go below zero. All the actions listed below allow the knight to gain experience points.

Here are some actions a knight can do:

- *recruit* a villager. This is possible if:
  - The knight does not have a companion already
  - The villager does not have a knight as a leader already
  - The knight can afford the recruiting cost for the villager. For example, if the villager cost is 3 and the knight has a bad reputation of -2, he would need 5 coins to recruit this villager. However, if the knight has a positive reputation of 5, he can recruit the villager for free.

The knight gains as many experience points as coins spent.

- *dismiss* a villager as a companion for free (gaining 5 experience points). This is only possible if the knight has a companion already.
- *heal* one or more wounds. The cost of healing is the same as the number of wounds to be healed; the knight must be able to afford the cost. For example, if the knight has 3 coins and a good reputation of 1, he can afford to heal up to 4 wounds. The knight gains as many experience points as wounds healed.

Your task is to add contracts to the deferred classes *KNIGHT* and *VILLAGER*, so that the informal specification above (together with the feature comments) is reflected in each class interface.

Please note:

- Assume that the void safety option of the compiler is turned off. This means that, when appropriate, you have to explicitly check whether the objects are void or not.
- The number of dotted lines is not indicative of the number of missing contract clauses.
- You need to write **True** at places where you think no explicit contract is necessary: leaving a postcondition empty gives you 0 point for that section.
- The following features from class *INTEGER* may be useful:

```
class INTEGER
feature
  max (other: INTEGER): INTEGER
    -- The greater of current object and 'other'.

    -- Other features omitted.
end
```

## 1.1 Solution

```
deferred class
  KNIGHT

feature -- Access

  wounds: INTEGER
    -- Number of wounds the current knight currently has.

  coins: INTEGER
    -- Number of coins owned. They are used to pay for recruiting and healing.

  reputation: INTEGER
    -- Affects positively or negatively the cost of recruiting and healing.

  experience: INTEGER
    -- Experience points gained by performing actions.

  companion: VILLAGER
    -- Companion of current knight, possibly Void.

feature -- Basic operations

  recruit ( a_villager : VILLAGER )
    -- Recruit a villager.
  require
    no_companion: companion = Void
    villager_exists : a_villager /= Void
    villager_is_recruitable : not a_villager.has_leader
    can_afford: coins >= a_villager.recruiting_cost - reputation
  deferred
  ensure
    villager_recruited : companion = a_villager
    villager_leader_set : a_villager.has_leader
    coins_updated: coins = old coins - (a_villager.recruiting_cost - reputation).
      max (0)
    experience_updated: experience = old experience - (coins - old coins)
  end

  dismiss
    -- Dismiss the current companion.
  require
    companion_exists: companion /= Void
  deferred
  ensure
    companion_dismissed: companion = Void
    villager_has_no_leader : not (old companion).has_leader
    experience_updated: experience = old experience + 5
  end

  heal (w: INTEGER)
```

```
    -- Heal w wounds.
  require
    heal_some_wounds: w > 0
    not_too_many_wounds_to_cure: w <= wounds
    can_afford: coins >= w - reputation
  deferred
  ensure
    wounds_updated: wounds = old wounds - w
    coins_updated: coins = old coins - (w - reputation).max(0)
    experience_updated: experience = old experience + w
  end

invariant
  wounds_non_negative: wounds >= 0
  coins_non_negative: coins >= 0
  reputation_in_range: reputation >= -5 and reputation <= 5
  experience_non_negative: experience >= 0
  binding_companionship: companion /= Void implies companion.has_leader

end

deferred class
  VILLAGER

  feature -- Access

    recruiting_cost : INTEGER
      -- Positive cost of recruiting the current villager .

  feature -- Status report

    has_leader: BOOLEAN
      -- Does the current villager have a leader?

  feature -- Status setting

    set_has_leader (hl: BOOLEAN)
      -- Set the "has leader" status for the current villager .
    require
      -- nothing
    deferred
    ensure
      has_leader_set: has_leader = hl
    end

  invariant
    recruiting_cost_positive : recruiting_cost > 0

end
```

## 2 Data Structures (10 points)

A *bag* (also called *multiset*) is a generalization of a set, where elements are allowed to appear more than once. For example, the bag  $\{a, a, b\}$  consists of two copies of  $a$  and one copy of  $b$ . However, a bag is still unordered, so the bags  $\{a, b, a\}$  and  $\{a, a, b\}$  are equivalent.

Below you will find source code of a linked representation of the bag data structure; this representation is very similar to a regular singly-linked list, except for the following:

- In addition to the value and the reference to the next cell, each bag cell stores the number of copies of its value (see Figure 1).
- For a given value, at most one cell storing that value should appear in the data structure.

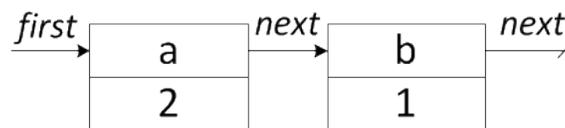


Figure 1: A possible linked representation of the bag  $\{a, a, b\}$ .

In the class `LINKED_BAG` below fill in the implementations of the following two features:

1. `remove (v: G; n: INTEGER)`, which removes as many copies of  $v$  as possible, up to  $n$ . For example, removing one copy of  $a$  from the bag  $\{a, a, b\}$  will result in a bag  $\{a, b\}$ , while removing two copies of  $c$  from the same bag will not change it.
2. `subtract (other: LINKED_BAG [G])`, which removes all elements of *other* from the current bag. For example, taking the bag  $\{a, a, b\}$  and subtracting  $\{a, b, c\}$  from it will yield the bag  $\{a\}$ .

Your implementation should satisfy the provided contracts.

### 2.1 Solution

```
class
  LINKED_BAG [G]

feature -- Access

  occurrences (v: G): INTEGER
    -- Number of occurrences of 'v'.

  local
    c: BAG_CELL [G]
  do
    from
      c := first
    until
      c = Void or else c.value = v
    loop
      c := c.next
    end
    if c /= Void then
      Result := c.count
    end
  end
```

```
    end
  end

feature -- Element change

  add (v: G; n: INTEGER)
    -- Add 'n' copies of 'v'.
    require
      n_positive: n > 0
    local
      c: BAG_CELL [G]
    do
      from
        c := first
      until
        c = Void or else c.value = v
      loop
        c := c.next
      end
      if c /= Void then
        c.set_count (c.count + n)
      else
        create c.make (v)
        c.set_count (n)
        c.set_next (first)
        first := c
      end
    ensure
      n_more: occurrences (v) = old occurrences (v) + n
    end

  remove (v: G; n: INTEGER)
    -- Remove as many copies of 'v' as possible, up to 'n'.
    require
      n_positive: n > 0
    local
      c, prev: BAG_CELL [G]
    do
      from
        c := first
      until
        c = Void or else c.value = v
      loop
        prev := c
        c := c.next
      end
      if c /= Void then
        if c.count > n then
          c.set_count (c.count - n)
        elseif c = first then
          first := first.next
        else
```

```
        prev.set_next (c.next)
    end
end
ensure
    n_less: occurrences (v) = (old occurrences (v) - n).max (0)
end

subtract (other: LINKED-BAG [G])
    -- Remove all elements of 'other'.
    require
        other_exists: other /= Void
    local
        c: BAG-CELL [G]
    do
        from
            c := other.first
        until
            c = Void
        loop
            remove (c.value, c.count)
            c := c.next
        end
    end
end

feature {LINKED-BAG} -- Implementation

    first: BAG-CELL [G]
        -- First cell.

end
```

### 3 Recursion (13 points)

#### Task 1

The function `n_th_element` (see below) should implement a recursive algorithm that, given a list `a`, computes the `n`-th element of a sorted list (in ascending order) that contains the same elements as the list `a`. Note that list `a` does not need to be sorted. See the example in task 2 to get an idea of what the correct output of function `n_th_element` should look like. *Complete the implementation by filling in the missing expressions. Note that the expected implementation uses recursion.*

#### Solution

```
if (not_greater.count + 1) = n then
  result := pivot
elseif (not_greater.count + 1) < n then
  result := n_th_element (greater, n - (not_greater.count + 1))
elseif n < (not_greater.count + 1) then
  result := n_th_element (not_greater, n)
end
```

#### Task 2

In the following code snippets, function `n_th_element` is called with different inputs. *Write down the output that is printed to the console for each snippet once function `n_th_element` has been properly implemented.* Note that the function `n_th_element` prints out the argument `n` in each call.

Assume that variable `a` was declared as follows:

```
local
  a: ARRAYED_LIST [INTEGER]
```

#### Example

```
create a.make (0) -- Create an empty list.
a.extend (1)
a.extend (2)
a.extend (-2)
print ("result = " + n_th_element (a, 1).out)
```

Output:

```
n = 1
n = 1
result = -2
```

#### Snippet 1

```
create a.make (0)
a.extend (0)
print ("result = " + n_th_element (a, 1).out)
```

Output:

.....

.....

.....

.....

.....

.....

**Solution**

```
n = 1  
result = 0
```

### Snippet 2

```
create a.make (0)
a.extend (5)
a.extend (1)
a.extend (3)
a.extend (2)
a.extend (1)
print ("result = " + n_th_element (a, 5).out)
```

Output:

.....  
.....  
.....  
.....  
.....  
.....

### Solution

```
n = 5
n = 3
n = 2
n = 1
result = 5
```