

# A CSP Model for Java Multithreading

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# Why Java needs a CSP model

- Many Java programs using threads seem to work correctly, but
  - Data races might be hidden
  - Deadlocks might not yet be detected
- How can we be sure that data races and deadlocks in fact cannot occur?

# Why Java needs a CSP model

- Solution: Model Java's synchronization facility in CSP
  - Allows us to reason in a formal way about its correct usage in Java programs
- Synchronization primitives of Java's client interface that are modelled:
  - **synchronized**
  - **wait()**, **notify()**, **notifyAll()**

# Java Monitors in CSP

- We model **synchronized** by the following CSP processes <sup>[1]</sup>:
  - **STARTSYNC**( o, me) = claim.o.me → **SKIP**
  - **ENDSYNC**( o, me) = release.o.me → **SKIP**

# Java Monitors in CSP

- `wait ()`, `notify ()`, `notifyAll ()` are modelled by the following CSP processes <sup>[1]</sup>:
  - **WAIT**(o, me) = `waita.o.me` → `release.o.me` →  
`waitb.o.me` → `claim.o.me` → **SKIP**
  - **NOTIFY**( o, me) = `notify.o.me` → **SKIP**
  - **NOTIFYALL**( o, me) = `notifyAll.o.me` → **SKIP**

# Java Monitors in CSP

- Java's internal monitor facility for an object  $o$  is modelled by <sup>[1]</sup>:
  - **MONITOR**(  $o$  ) = **MLOCK**(  $o$  ) || **MWAIT**(  $o$ , { } )
  - **MLOCK**(  $o$  ) =  $\text{claim.o?t} \rightarrow \text{MLOCKED}( o, t )$
  - **MLOCKED**(  $o$ ,  $t$  ) =  $\text{release.o.t} \rightarrow \text{MLOCK}( o )$ 
    - $\text{notify.o.t} \rightarrow \text{MLOCKED}( o, t )$
    - $\text{notifyall.o.t} \rightarrow \text{MLOCKED}( o, t )$
    - $\text{waita.o.t} \rightarrow \text{MLOCKED}( o, t )$

# Java Monitors in CSP

- **MWAIT** (using **RELEASE**) is defined as follows <sup>[1]</sup>:
  - **MWAIT**( o, ws) = (waita.o?t → **MWAIT**( o, ws ∪ {t}))
    - (notify.o?t → **if** (|ws| > 0) **then**
      - $\prod_{s \in ws} \text{waitb.o!s} \rightarrow \mathbf{MWAIT}( o, ws - \{s\})$
      - else**
        - MWAIT**( o, {}))
    - (notifyall.o?t → **RELEASE**( o, ws))
  - **RELEASE**( o, ws) = **if** (|ws| > 0) **then**
    - $\prod_{t \in ws} \text{waitb.o!t} \rightarrow \mathbf{RELEASE}( o, ws - \{t\})$
    - else**
      - MWAIT**( o, {})

# Case Study

## CSP model of One2OneChannel

- So far we have set up our CSP model of Java's synchronization facility
- Let's apply our CSP model to an example: The One2OneChannel of JCSP



# Case Study

## CSP model of One2OneChannel

- Allows exactly two threads to communicate with each other
- Communication complies with rendez-vous pattern
  - Reading thread and writing thread meet at some point in time
- Internal attributes:
  - **Object channel\_hold** : Data being transmitted via the channel
  - **boolean channel\_empty** : Indicates whether channel is empty
- Methods:
  - **public Object synchronized read()**
  - **public synchronized void write( Object mess)**

# Case Study

## CSP model of One2OneChannel

- Variables (restricted to boolean values) are managed by the **VARIABLE** process as follows <sup>[1]</sup>:
  - **VARIABLE**( o, v) = **VAR2**( o, v, TRUE)
  - **VAR2**( o, v, d) = (
    - $\text{getvar.o.v.t!d} \rightarrow \text{VAR2}( o, v, d)$   
t ∈ Threads
    - ( □  $\text{setvar.o.v.t?x} \rightarrow \text{VAR2}( o, v, x)$   
t ∈ Threads)
  - **VARIABLES**( o) = **VARIABLE**( o, channel\_empty)  
|| **VARIABLE**( o, channel\_hold)

# Case Study

## CSP model of One2OneChannel

### Java Code

```
public synchronized Object read()  
throws InterruptedException{  
    if (channel_empty) {  
        channel_empty = false;  
        wait();  
        notify();  
    }else{  
        channel_empty = true;  
        notify();  
    }  
  
    return channel_hold;  
}
```

### CSP Model

# Case Study

## CSP model of One2OneChannel

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public synchronized Object read()  
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        notify();  
    }  
  
    return channel_hold;  
}
```

### CSP Model

```
READ( o, t) =  
    ready.o.t → claim.o.t → release.o.t →  
    READ( o, t)
```

# Case Study

## CSP model of One2OneChannel

### Java Code

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        notify();  
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}
```

### CSP Model

```
READ( o, t) =  
    ready.o.t → claim.o.t →  
    getvar.o.channel_empty.t?c → (  
    if (c = TRUE) then  
    else  
    ); → release.o.t → READ( o, t)
```

# Case Study

## CSP model of One2OneChannel

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throws InterruptedException{  
    if (channel_empty) {  
        channel_empty = false;  
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    }else{  
        channel_empty = true;  
        notify();  
    }  
  
    return channel_hold;  
}
```

### CSP Model

```
READ( o, t) =  
    ready.o.t → claim.o.t →  
    getvar.o.channel_empty.t?c → (  
        if (c = TRUE) then  
            setvar.o.channel_empty.t!FALSE  
        else  
            setvar.o.channel_empty.t!TRUE  
    ); getvar.o.channel_hold.t?mess →  
    release.o.t → read.o.t!mess →  
    READ( o, t)
```

# Case Study

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throws InterruptedException{  
    if (channel_empty) {  
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    ready.o.t → claim.o.t →  
    getvar.o.channel_empty.t?c → (  
    if (c = TRUE) then  
        setvar.o.channel_empty.t!FALSE →  
        WAIT( o, t); NOTIFY( o, t)  
    else  
        setvar.o.channel_empty.t!TRUE →  
        NOTIFY( o, t)  
    ); getvar.o.channel_hold.t?mess →  
    release.o.t → read.o.t!mess →  
    READ( o, t)
```

# Case Study

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### CSP Model

```
READ( o, t) =  
    ready.o.t → claim.o.t →  
    getvar.o.channel_empty.t?c → (  
    if (c = TRUE) then  
        setvar.o.channel_empty.t!FALSE →  
        WAIT( o, t); NOTIFY( o, t)  
    else  
        setvar.o.channel_empty.t!TRUE →  
        NOTIFY( o, t)  
    ); getvar.o.channel_hold.t?mess →  
    release.o.t → read.o.t!mess →  
    READ( o, t)
```



# Case Study

## CSP model of One2OneChannel

- CSP model of write method similar to that of read method
- The final JCSP One2OneChannel is <sup>[1]</sup>:
  - **JCSPCHANNEL**( o, t<sub>1</sub>, t<sub>2</sub>) = **READ**( o, t<sub>1</sub>) || **WRITE**( o, t<sub>2</sub>) ||  
**MONITOR**( o) || **VARIABLES**( o)
- It is still possible that a thread, for which the channel is not destined, tries to access the channel

# Case Study

## Simplified Model of One2OneChannel

- The previous model of the One2OneChannel is simplified such that monitors are no longer needed
- The simplified model represents the One2OneChannel by two processes
  - **LEFT** process: Models ending to which input is written
  - **RIGHT** process: Models ending from which output is read

# Case Study

## Simplified Model of One2OneChannel

- The simplified channel is defined as follows <sup>[1]</sup>:
  - $\text{CHANNEL}(o, t_1, t_2) = (\text{LEFT}(o, t_2) \parallel \text{RIGHT}(o, t_1)) \setminus \{\text{transmit.o.m} \mid m \in \text{Data}\}$
  - $\text{LEFT}(o, t_1) = \text{write.o.t}_1?mess \rightarrow \text{transmit.o!mess} \rightarrow \text{ack.o.t}_1 \rightarrow \text{LEFT}(o, t_1)$
  - $\text{RIGHT}(o, t_2) = \text{ready.o.t}_2 \rightarrow \text{transmit.o?mess} \rightarrow \text{read.o.t}_2!mess \rightarrow \text{RIGHT}(o, t_2)$

# Case Study

## Simplified Model of One2OneChannel

- Equivalence of the simplified model and the original model was verified using FDR
- From now on, we can therefore rely on the simplified model instead of the more complex model of the One2OneChannel
  - Makes reasoning about it easier

# Conclusion

- CSP model of Java's synchronization facility can be incorporated to build CSP models of Java programs
- Reasoning about absence of deadlocks as well as data races possible using the CSP model
- Verifying equivalence of complex to simplified models possible

# References

- [1] Peter H. Welch and Jeremy M. R. Martin. 2000. A CSP Model for Java Multithreading. *International Symposium on Software Engineering for Parallel and Distributed Systems (PDSE)*. 114-122.

Questions?