A Sound and Complete Program Logic for Eiffel

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Abstract. Object-oriented languages provide advantages such as reuse and modularity, but they also raise new challenges for program verification. Program logics have been developed for languages such as C# and Java. However, these logics do not cover the specifics of the Eiffel language. This paper presents a program logic for Eiffel that handles exceptions, once routines, and multiple inheritance. The logic is proven sound and complete w.r.t. an operational semantics. Lessons on language design learned from the experience are discussed.

Key words: Software verification, program proofs, operational semantics, Eiffel

1 Introduction

Program verification relies on a formal semantics of the programming language, typically a program logic such as Hoare logic. Program logics have been developed for mainstream object-oriented languages such as Java and C#. For instance, Poetzsch-Heffter and Müller presented a Hoare-style logic for a subset of Java [18]. This logic includes the most important features of object-oriented languages such as abstract types, dynamic binding, subtyping, and inheritance. However, exception handling is not treated in their work. Huisman and Jacobs [4] developed a Hoare-stype logic which handles abrupt termination. It includes not only exception handling but also break, continue, and return statements. Their logic was developed to verify Java-like programs.

Eiffel has several distinctive features not present in mainstream languages, for instance, a different exception handling mechanism, once routines, and multiple inheritance. Eiffel's once routines (methods) are used to implement global behavior, similarly to static fields and methods in Java. Only the first invocation of a once routine triggers an execution of the routine body; subsequent invocations return the result of the first execution. The development of formal techniques for these concepts does not only allow formally verifying Eiffel programs, but also allows comparing the different concepts, and analyzing which concepts are more suitable to be applied for formal verification.

The main contributions of this paper are an operational and an axiomatic semantics for Eiffel, and soundness and completeness results. The semantics in-

cludes: (1) basic instructions such as loops, compounds and assignments; (2) routine invocations; (3) exceptions; (4) once routines, and (5) multiple inheritance. During this work, we have found that Eiffel's exception mechanism was not ideal for formal verification. The use of retry instructions in a rescue clause complicates its verification. For this reason, a change in the Eiffel exception handling mechanism has been proposed, and will be adopted by a future revision of the language standard.

Outline. Section 2 describes the subset of Eiffel and its operational semantics. Section 3 presents the Eiffel program logic. An example that illustrates the use of the logic is described in Section 4. The soundness and completeness theorems are presented in Section 5. Section 6 discusses related work. Finally, in Section 7 we compare the Eiffel features such as exception handling and once routines with other object-oriented languages features such as try-catch instructions and static methods. Proof of soundness and completeness for our logic are presented in a technical report [11].

2 A Semantics for Eiffel

2.1 The Source Language

The source language is a subset of Eiffel, which includes the most important features of Eiffel, although agents are omitted being beyond the scope of this work. The most interesting concepts supported by this subset are: (1) multiple inheritance, (2) exception handling, and (3) once routines.

An Eiffel program is a sequence of class declarations. A class declaration consist of an optional inheritance clause, and a class body. The inheritance clause supports multiple inheritance, and allows undefining, redefining, and renaming routines. If the routine is redefined, preconditions of subclasses can be weaker, and postconditions can be stronger. A class body is a sequence of attribute declarations or routine declarations. For simplicity, routines are functions that take always one argument and return a result. However, we do not assume that functions are side-effect free, that is, our logic fully handles heap modifications. The source language also supports once routines.

The syntax of the subset of Eiffel is presented in Figure 1. Class names, routine names, variables and attributes are denoted by ClassId, RoutineId, VarId, and AttributeId, respectively. The set of variables is denoted by Var; VarId is an element of Var. The arithmetic functions * and + are defined as usual, and list_of denotes a comma-separated list. For space restrictions, we omit attribute reading, attribute writing, and object creation here, but these features are presented in our technical report [11].

Boolean expressions and expressions (BoolExp and Exp) are side-effect-free, and do not trigger exceptions¹. In addition, we write ExpE for the expressions which might raise exceptions. For simplicity, expressions ExpE are only allowed

¹ the necessary checks are delegated to the compiler.

in assignments. This assumption simplifies the presentation of the logic, especially the rules for routine invocation, if then else, and loop instructions. However, the logic could be easily extended.

One of the design goals of our logic is that programs behave in the same way when contracts are checked at runtime and when they are not. For this reason, we demand that expressions occurring in contracts to be side-effect-free, and to not trigger exceptions.

```
Program
           ::= ClassDecl*
           ::= class ClassId [inherit Parent+] MemberDecl* end
ClassDecl
Type
           ::= boolT
                         int T
                                | ClassId
                                           \mid voidT
Parent
                     [Undefine]
                                [Redefine]
                                           [Rename]
           ::= Type
Undefine
           ::= undefine list\_of\ RoutineId
Redefine
           ::= redefine list\_of RoutineId
Rename
           ::= rename list\_of (RoutineId as RoutineId)
MemberDecl ::= AttributeId Type | Routine
           ::= RoutineId (VarId : Type) : Type
Routine
                 require\ BoolExp
                 [local list\_of (VarId: Type)]
                 (do | once)
                   Instr
                 [rescue Instr]
                 ensure BoolExp
                 end
Instr
           ::= VarId := ExpE
                                 Instr; Instr
                                              | check BoolExp end
              from invariant BoolExp until BoolExp loop Instr end
               if BoolExp then Instr else Instr end
               VarId := VarId.Type : RoutineId (Exp)
Exp, ExpE
           ::= Literal | VarId | Exp Op Exp | BoolExp
BoolExp
           ::= Literal | VarId | BoolExp Bop BoolExp | Exp CompOp Exp
Op
           Bop
           ::= and | or | xor | and then | or else | implies
           ::= < | > | <= | >= | = | /=
CompOp
```

Fig. 1. Syntax of the subset of Eiffel.

2.2 The Memory Model

The state of an Eiffel program describes the current values of local variables, arguments, the current object, and the current object store \$. A value is either a boolean, or an integer, or the void value, or an object reference. An object is characterized by its class and an identifier of infinite sort *ObjId*. The data type *Value* models values; its definition is the following:

data type Value = boolV Bool | intV Int | objV ClassId ObjId | voidV

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The function τ : $Value \rightarrow Type$ returns the dynamic type of a value, where $\tau(\mathbf{boolV}\ b) = boolT;\ \tau(\mathbf{intV}\ n) = intT;\ \tau(\mathbf{objV}\ cId\ oId) = cId;$ and $\tau(\mathbf{voidV}) = voidT.$

The state of an object is defined by the values of its attributes. The sort Attribute defines the attribute declaration T@a where a is an attribute declaration in the class T. We use a sort Location, and a function instvar where instvar(V, T@a) yields the instance of the attribute T@a if V is an object reference, and the object has an attribute T@a; otherwise it yields undef. The datatype definitions and the signature of instvar are the following:

```
data type Attribute = Type \ AttributeId
data type Location = ObjId \ AttributeId
instvar : Value \times Attribute \rightarrow Location \cup \{undef\}
```

The object store models the heap describing the states of all objects in a program at a certain point of execution. An object store is modeled by an abstract data type ObjectStore. We use the object store presented by Poetzsch-Heffter and Müller [17, 18]. The following operations apply to the object store: os(l) denotes reading the location l in the object store os; alive(o, os) yields true if and only if object o is allocated in the object store os; new(os, C) yields a reference of type C to a new object in the store os; os < l := v > updates the object store os at the location l with the value v; os < C > denotes the store after allocating a new object of type C. An axiomatization of these functions is presented in [17].

```
 \begin{array}{c} \text{-(-)}: ObjectStore \times Location \rightarrow Value \\ alive: Value \times ObjectStore \rightarrow Bool \\ new: ObjectStore \times ClassId \rightarrow Value \\ \text{-<-}:=->: ObjectStore \times Location \times Value \rightarrow ObjectStore \\ \text{-<-}:>: ObjectStore \times ClassId \rightarrow ObjectStore \\ \end{array}
```

2.3 Operational Semantics

Program states are a mapping from local variables and arguments to values, and from the current object store \$ to ObjectStore. The program state is defined as follows:

```
State \equiv Local \times Heap

Local \equiv VarId \cup \{Current, p, Result, Retry\} \rightarrow Value \cup \{undef\}

Heap \equiv \{\$\} \rightarrow ObjectStore
```

Local maps local variables, the receiver object Current (this in Java), arguments, Result, and Retry to values. Arguments are denoted by p. The variables Result and Retry are special variables used to store the result value, and the retry value but they are not part of VarId. For this reason, these variables are included explicitly.

For $\sigma \in State$, $\sigma(e)$ denotes the evaluation of the expression e in the state σ . Its signature is the following:

$$\sigma: ExpE \rightarrow Value \cup \{exc\}$$

The evaluation of an expression e can yield exc meaning that an exception was triggered in e. For example, $\sigma(x/0)$ yields exc. Furthermore, the evaluation $\sigma(y \neq 0 \land x/y = z)$ is different from exc because σ first evaluates $y \neq 0$ and then evaluates x/y = z only if $y \neq 0$ evaluates to true. The state $\sigma[x := V]$ denotes the state obtained after the replacement of x by V in the state σ .

The transitions of the operational semantics have the form: $\langle \sigma, S \rangle \to \sigma', \chi$ where σ and σ' are states, S is an instruction, and χ is the current status of the program. The value of χ can be either the constant *normal* or *exc*. The variable χ is required to treat abrupt termination. The transition σ , $S \to \sigma'$, normal expresses that executing the instruction S in the state σ terminates normally in the state σ' . The transition σ , $S \to \sigma'$, *exc* expresses that executing the instruction S in the state σ terminales with an exception in the state σ' .

In the following, we present the operational semantics. First, we present the operational semantics for basic instructions. Second, we define the semantics for routine invocation. Finally, we show the semantics for exception handling and once routines. The operational semantics for exception handling and once routines is one of the contributions of this paper.

Basic Instructions. Figure 2 presents the operational semantics for basic instructions such as assignment, compound, conditional, and loop instructions. The operational semantics for assignment, conditional, and loop instructions is standard. Compound is defined by two rules: in rule (2.3) the instruction s_1 is executed and an exception is triggered. The instruction s_2 is not executed, and the state of the compound is the state produced by s_1 . In rule (2.4), s_1 is executed and terminates normally. The state of the compound is the state produced by s_2 .

The check instruction helps to express a property that one believes will be satisfied. If the property is satisfied then the system does not change. If the property is not satisfied then an exception is triggered. The semantics for check consist of two rules: if the condition of the check instruction evaluates to true, then the instruction terminates normally, rule (2.5); otherwise the check instruction triggers an exception, rule (2.6).

Routine Invocations. Poetzsch-Heffter and Müller [18] have developed an operational and axiomatic semantics for a Java-like languages which handle inheritance, dynamic binding, subtyping and abstract types. However, the source language used in their work has single inheritance. In this section, we extend their logic to support multiple inheritance.

Poetzsch-Heffter and Müller distinguish between virtual routines and routine implementation. A class T has a *virtual routine* T:m for every routine m that it declares or inherits. A class T has a *routine implementation* T@m for every routine m that it defines (or redefines). We assume in the following that every

Assignment instruction
$$\frac{\sigma(e) = exc}{\langle \sigma, x := e \rangle \to \sigma, exc} (2.1) \qquad \frac{\sigma(e) \neq exc}{\langle \sigma, x := e \rangle \to \sigma[x := \sigma(e)], normal} (2.2)$$

Compound

$$\frac{\langle \sigma, s_1 \rangle \to \sigma', exc}{\langle \sigma, s_1; s_2 \rangle \to \sigma', exc} (2.3) \qquad \frac{\langle \sigma, s_1 \rangle \to \sigma', normal \quad \langle \sigma', s_2 \rangle \to \sigma'', \chi}{\langle \sigma, s_1; s_2 \rangle \to \sigma'', \chi} (2.4)$$

Check Instruction

$$\frac{\sigma(e) = true}{\langle \sigma, \text{check } e \text{ end} \rangle \to \sigma, normal} (2.5) \frac{\sigma(e) = false}{\langle \sigma, \text{check } e \text{ end} \rangle \to \sigma, exc} (2.6)$$

Conditional Instruction

$$\frac{\sigma(e) = true \quad \langle \sigma, s_1 \rangle \to \sigma', \chi}{\langle \sigma, \text{if } e \text{ then } s_1 \text{ else } s_2 \text{ end} \rangle \to \sigma', \chi} (2.7)$$

$$\frac{\sigma(e) = false \quad \langle \sigma, s_2 \rangle \to \sigma', \chi}{\langle \sigma, \text{if } e \text{ then } s_1 \text{ else } s_2 \text{ end} \rangle \to \sigma', \chi} (2.8)$$

Loop Instruction

$$\frac{\sigma(e) = true}{\langle \sigma, \text{from invariant } I \text{ until } e \text{ loop } s_1 \text{ end} \rangle \to \sigma, normal}$$
(2.9)

$$\frac{\sigma(e) = false \quad \langle \sigma, s_1 \rangle \to \sigma', exc}{\langle \sigma, \text{from invariant } I \text{ until } e \text{ loop } s_1 \text{ end} \rangle \to \sigma', exc} (2.10)$$

$$\sigma(e) = false \qquad \langle \sigma, s_1 \rangle \to \sigma', normal \\ \langle \sigma', \text{from invariant } I \text{ until } e \text{ loop } s_1 \text{ end} \rangle \to \sigma'', \chi \\ \hline \langle \sigma, \text{from invariant } I \text{ until } e \text{ loop } s_1 \text{ end} \rangle \to \sigma'', \chi$$

Fig. 2. Operational Semantics for Basic Instructions

invocation is decorated with the virtual method being invoked. The semantics of routine invocations uses two functions: body and impl. The function impl(T,m) yields the implementation of routine m in class T. This implementation could be defined by T or inherited from a superclass. The function body yields the instruction constituting the body of a routine implementation. The signatures of these functions are as follows:

$$impl: Type \times RoutineId \rightarrow RoutineImpl \cup \{undef\}$$

 $body: RoutineImpl \rightarrow Instr$

The complications of multiple inheritance can be elegantly captured by a revised definition of impl. While impl(T, m) traverses T's parent classes, it can take redefinition, undefinition, and renaming into account. In particular, impl is

undefined for deferred routines (abstract methods) or when an inherited routine has been undefined.

```
class A
                                                   class B
    \mathbf{feature}\ m\ \mathbf{do}\ ...\ \mathbf{end}
                                                       feature m do ... end
end
                                                   end
class C
{\bf inherit} \ \ A
              rename m as n end
end
                                                   class E
{\bf class} \quad D
                                                   inherit C rename m as m2 end
inherit C redefine m end
    \mathbf{feature}\ m\ \mathbf{do}\ ...\ \mathbf{end}
                                                   end
end
```

Fig. 3. Example of Inheritance using Rename and Redefine.

Figure 3 shows an example of inheritance using the features **rename** and **redefine**. Table 1 presents an example of the application of the function *impl* using the class declarations of Figure 3. For brevity, refer to our technical report [11] for a definition of *impl*.

Table 1. Example of the Application of the Function *impl*.

	$\overline{\mathrm{impl}(\mathrm{D,m})} = \mathrm{D@m}$
impl(A,m) = A@m	1 () /
impl(B,m) = B@m	impl(D,n) = B@m
	impl(E,m) = undefined
impl(C,m) = A@m	impl(E,m2) = A@m
impl(C,n) = B@m	impl(E,n) = B@m
	$\operatorname{Imp}(\mathbf{E},\mathbf{n}) = \mathbf{D} \otimes \mathbf{m}$

The operational semantics of routine invocation for non-once routines is defined with the following rules:

T:m is not a once routine
$$\frac{\sigma(y) = voidV}{\langle \sigma, x := y.T:m(e) \rangle \to \sigma, exc}$$
(1)

$$T:m \text{ is not a once routine} \\ \sigma(y) \neq voidV \qquad \langle \sigma[Current := \sigma(y), p := \sigma(e)], body(impl(\tau(\sigma(y)), m)) \rangle \rightarrow \sigma', \chi \\ \langle \sigma, x := y. T: m(e) \rangle \rightarrow \sigma'[x := \sigma'(Result)], \chi$$
(2)

In rule (1), since the target y is Void, the state σ is not changed and an exception is triggered. In rule (2), the target is not Void, thus, the *Current*

object is updated with y, and the argument p by the expression e, and then the body of the routine is executed. To handle dynamic dispatch, first, the dynamic type of y is obtained using the function τ . Then, the routine implementation is determined by the function impl. Finally, the body of the routine is obtained by the function body. Note that multiple inheritance is handled using the function impl, which yields the appropriate routine implementation for m.

Exception Handling. Exceptions [7] raise some of the most interesting problems addressed in this paper. A routine execution either succeeds - meaning that it terminates normally - or fails, triggering an exception. An exception is an abnormal event, which occurred during the execution. To treat exceptions, each routine may contain a rescue clause. If the routine body is executed and terminates normally, the rescue clause is ignored. However, if the routine body triggers an exception, control is transferred to the rescue clause. Each routine defines a boolean local variable *Retry* (in a similar way as for *Result*). If at the end of the clause the variable *Retry* has value true, the routine body (do clause) is executed again. Otherwise, the routine fails, and triggers an exception. If the rescue clause triggers another exception, the second one takes precedence and it can be handled through the rescue clause of the caller. The *Retry* variable can be assigned to in either a do clause or a rescue clause.

The operational semantics for the exception handling mechanism is defined by rules 3-6 below. If the execution of s_1 terminates normally, then the rescue block is not executed, and the returned state is the one produced by s_1 (rule 3). If s_1 terminates with an exception, and s_2 triggers another exception, the rescue terminates in an exception returning the state produced by s_2 (rule 4). If s_1 triggers an exception and s_2 terminates normally but the *Retry* variable is false, then the rescue terminates with an exception returning the state produced by s_2 (rule 5). In the analogous situation with *Retry* being true, the rescue is executed again and the result is the one produced by the new execution of the rescue (rule 6). Note that the rescue is a loop that iterates over s_2 ; s_1 until s_1 terminates normally or *Retry* is false.

$$\frac{\langle \sigma, s_1 \rangle \to \sigma', normal}{\langle \sigma, s_1 \text{ rescue } s_2 \rangle \to \sigma', normal}$$
(3)

$$\frac{\langle \sigma, s_1 \rangle \to \sigma', exc \quad \langle \sigma', s_2 \rangle \to \sigma'', exc}{\langle \sigma, s_1 \text{ rescue } s_2 \rangle \to \sigma'', exc}$$
(4)

$$\frac{\langle \sigma, s_1 \rangle \to \sigma', exc \quad \langle \sigma', s_2 \rangle \to \sigma'', normal \quad \neg \sigma''(Retry)}{\langle \sigma, s_1 \text{ rescue } s_2 \rangle \to \sigma'', exc}$$
 (5)

$$\frac{\langle \sigma, s_1 \rangle \to \sigma', exc \quad \langle \sigma', s_2 \rangle \to \sigma'', normal \quad \sigma''(Retry)}{\langle \sigma'', s_1 \text{ rescue } s_2 \rangle \to \sigma''', \chi}$$

$$\frac{\langle \sigma, s_1 \text{ rescue } s_2 \rangle \to \sigma''', \chi}{\langle \sigma, s_1 \text{ rescue } s_2 \rangle \to \sigma''', \chi}$$
(6)

Once Routines. The mechanism used in Eiffel to access a shared object is *once* routines. This section focuses on once functions; once procedures are similar. The semantics of once functions is as follows. When a once function is invoked for the first time in a program execution, its body is executed and the outcome is cached. This outcome may be a result in case the body terminates normally or an exception in case the body triggers an exception. For subsequent invocations, the body is not executed; the invocations produce the same outcome (result or exception) like the first invocation. Note that whether an invocation is the first or a subsequent one is determined solely by the routine implementation name.

To be able to develop a semantics for once functions, finally, we also need to consider recursive invocations. As described in the Eiffel ECMA standard [8], a recursive call may start before the first invocation finished. In that case, the recursive call will return the result that has been obtained so far. The mechanism is not so simple. For example the behavior of following recursive factorial function might be surprising:

```
 \begin{array}{lll} \textit{factorial} & (i: \ INTEGER): \ INTEGER \\ 2 & \ \textbf{require} \ i>=0 \\ & \ \textbf{once} \\ 4 & \ \textbf{if} \ i<=1 \ \textbf{then} \ \textbf{Result} := 1 \\ & \ \textbf{else} \\ 6 & \ \textbf{Result} := i \\ & \ \textbf{Result} := \textbf{Result} * \textit{factorial} \ (i-1) \\ 8 & \ \textbf{end} \\ & \ \textbf{end} \end{array}
```

This example is a typical factorial function but it is also a once function, and the assignment Result := i*factorial(i-1) is split into two separate assignments. If one invokes factorial(3) we observe that the returned result is 9. The reason is that the first invocation, factorial(3), assigns 3 to Result. This result is stored for a later invocation since the function is a once function. Then, the recursive call is invoked with argument 2. But this invocation is not the first invocation, so the second invocation returns the stored value (in this case 3). Thus, the result of invoking factorial(3) is 3*3. If we do not split the assignment, the result would be 0 because factorial(2) would return the result obtained so far which is the default value of factorial(3). This corresponds to a semantics where recursive calls are replaced by factorial(3).

To be able to develop a sound semantics for once functions, we need to consider all the possible cases described above. To fulfil this goal, we present a pseudo-code of once functions. Given a once function m with body b, the pseudo-code is the following:

```
1    if not m_done then m_done := true; execute the body b
        if body triggers an exception e then m_exception := e end
3    end
    if m_exception /= Void then throw m_exception else Result := m_result
5    end
```

We assume the variables m_done , $m_exception$ and m_result are global variables, which exist one per routine implementation and can be shared by all invocations of that function. Furthermore, we assume the body of the function sets the result variable m_result . Now, we can see more clearly why the invocation of factorial (3) returns 9. In the first invocation, first the global variable m_done is set to false, and then the function's body is executed. The second invocation returns the stored value 3 because m_done is false.

To define the semantics for once functions, we introduce global variables to store the information whether the function was invoked before or not, to store whether it triggers an exception or not, and to store its result. These variables are $T@m_done$, $T@m_result$, and $T@m_exc$. There is only one variable $T@m_done$ per every routine implementation T@m. Descendants of the class T that do not redefine the routine m inherit the routine implementation T@m, therefore they share the same global variable $T@m_done$.

Given a once function m implemented in the class T, $T@m_done$ returns true if the once function was executed before, otherwise it returns false; $T@m_result$ returns the result of the first invocation of m; and $T@m_exc$ returns true if the first invocation of m produced an exception, otherwise it returns false. Since the type of the exception is not used in the exception mechanism, we use a boolean variable $T@m_exc$, instead of a variable of type EXCEPTION. We omit the definition of a global initialization phase $T@m_done = false$, $T@m_result = default\ value$, and $T@m_exc = false$. This initialization is performed in the make routine of the ROOT class.

The invocation of a once function is defined in four rules (rules 7-10, Figure 4). Rule (7) describes the normal execution of the first invocation of a once function. Before its execution, the global variable $T@m_done$ is set to true. Then, the function body is executed. We assume here that the body updates the variable $T@m_result$ whenever it assigns to Result. Rule (8) models the first invocation of an once function that terminates with an exception. The function is executed and terminates in the state σ' . The result of the once function m is the state σ' where the variable $T@m_exc$ is set to true to express that an exception was triggered. In rule 9, the first invocation of the once function terminates normally, the remaining invocations restore the stored value using the variable $T@m_result$. In rule 10, the first invocation of m terminates with an exception, so the subsequent invocations of m trigger an exception, too.

3 A Program Logic for Eiffel

The logic for Eiffel is based on the programming logic presented by Poetzsch-Heffter and Müller [18, 19]. We take over many of the rules, especially all the language-independent rules such as the rules of consequence. We do not repeat those rules here. We have developed new rules to model exceptions and once routines. Poetzsch-Heffter et al. [19] uses a special variable χ to capture the status of the program such as normal or exceptional status. We instead use Hoare triples with two postconditions to encode the status of the program execution.

$$T@m = impl(\tau(\sigma(y)), m) \quad T@m \text{ is a once routine}$$

$$\sigma(T@m_done) = false$$

$$\langle \sigma[T@m_done := true, Current := y, p := \sigma(e)], body(T@m)\rangle \to \sigma', normal$$

$$\langle \sigma, x := y.S:m(e)\rangle \to \sigma'[x := \sigma'(Result)], normal$$

$$T@m = impl(\tau(\sigma(y)), m) \quad T@m \text{ is a once routine}$$

$$\sigma(T@m_done) = false$$

$$\langle \sigma[T@m_done := true, Current := y, p := \sigma(e)], body(T@m)\rangle \to \sigma', exc$$

$$\langle \sigma, x := y.S:m(e)\rangle \to \sigma'[T@m_exc := true], exc$$

$$T@m = impl(\tau(\sigma(y)), m) \quad T@m \text{ is a once routine}$$

$$\sigma(T@m_done) = true$$

$$\sigma(T@m_exc) = false$$

$$\langle \sigma, x := y.S:m(e)\rangle \to \sigma[x := \sigma(T@m_result)], normal$$

$$T@m = impl(\tau(\sigma(y)), m) \quad T@m \text{ is a once routine}$$

$$\sigma(T@m_exc) = false$$

$$\sigma(T@m_exc) = true$$

$$\sigma(T@m_done) = true$$

$$\sigma(T@m_done) = true$$

$$\sigma(T@m_exc) = true$$

$$\sigma(T$$

Fig. 4. Operational Semantics for Once Routines

The logic is a Hoare-style logic. Properties of routines and routine bodies are expressed by Hoare triples of the form $\{P\}$ S $\{Q_n, Q_e\}$, where P, Q_n, Q_e are formulas in first order logic, and S is a routine or an instruction. The third component of the triple consists of a normal postcondition (Q_n) , and an exceptional postcondition (Q_e) .

The triple $\{P\}$ S $\{Q_n, Q_e\}$ defines the following refined partial correctness property: if S's execution starts in a state satisfying P, then (1) S terminates normally in a state where Q_n holds, or (2) S throws an exception and Q_e holds, or (3) S aborts due to errors or actions that are beyond the semantics of the programming language, e.g., memory allocation problems, or (4) S runs forever.

Boolean Expressions. Preconditions and postcondition are formulas in first order logic. Since expressions in assignments can trigger exceptions, we cannot always use these expressions in pre- and postconditions of Hoare triples. For example, if we want to apply the substitution P[e/x] where e is an ExpE expression, first, we need to check that e does not trigger any exception, and then we can apply the substitution. To do this, we introduce a function safe that takes an expression, and yields a safe expression. A safe expression is an expression whose evaluation does not trigger an exception. The definition of safe expression is the following:

Definition 1 (Safe Expression). An expression e is a **safe expression** if and only if $\forall \sigma : \sigma(e) \neq exc$.

Definition 2 (Function Safe). The function safe: $ExpE \rightarrow Exp$ returns an expression that expresses if the input expression is safe or not. The definition of this function is the following:

```
safe: ExpE \rightarrow Exp

safe (e_1 \ oper \ e_2) = safe(e_1) \land safe(e_2) \land safe\_op (oper, e_1, e_2)

safe\_op: op \times ExpE \times ExpE \rightarrow Exp

safe\_op (oper, e_1, e_2) = \mathbf{if} (oper = //) \mathbf{then} (e_2 \neq 0) \mathbf{else} \ true
```

Lemma 1. For each expression e, safe(e) satisfies:

```
- safe(e) is a safe expression
- \sigma(safe(e)) = true \Leftrightarrow \sigma(e) \neq exc
```

Lemma 2 (Substitution). If the expression e is a safe expression, then:

$$\forall \ \sigma : (\sigma \models P[e/x] \Leftrightarrow \sigma[x := \sigma(e)] \models P)$$

We define $\sigma \models P$ as the usual definition of \models in first order logic but with the restriction that the expressions in P are safe expressions.

Signatures of Contracts. Contracts refer to attributes, variables and types. We introduce a signature Σ that represents the constant symbols of these entities. Given an Eiffel program, Σ denotes the signature of sorts, functions and constant symbols as described in Section 2.1. Arguments, program variables, and the current object store \$ are treated syntactically as constants of Value and ObjectStore. Preconditions and postconditions of Hoare triples are formulas over $\Sigma \cup \{Current, p, Result, Retry\} \cup Var(r)$ where r is a routine, and Var(r) denotes the set of local variables of r. Note that we assume Var(r) does not include the Result variable and the Retry variable, it only includes the local variables declared by the programmer. Routine preconditions are formulas over $\Sigma \cup \{Current, p, \$\}$, and routine postconditions are formulas over $\Sigma \cup \{Current, p, Result, Retry, \$\}$.

We treat recursive routines in the same way as Poetzsch-Heffter and Müller [18] We use *sequents* of the form $\mathcal{A} \triangleright \mathbf{A}$ where \mathcal{A} is a set of routine annotations and \mathbf{A} is a triple. Triples in \mathcal{A} are called assumptions of the sequent, and \mathbf{A} is called the consequent of the sequent. Thus, a sequent expresses that we can prove a triple based on the assumptions about routines.

In the following, we present the logic for Eiffel. First, we present the basic instructions. Second, we define the logic for invocation. Finally, we present the semantics for exception handling and once routines. The logic for exception handling and once routines is another contribution of this paper.

3.1 Basic Rules

Figure 5 presents the axiomatic semantics for basic instructions such as assignment, compound, loop, and conditional instructions. In the assignment rule, if

the expression e is safe (it does not throw any exception) then the precondition is obtained replacing x by e in P. Otherwise the precondition is the exceptional postcondition.

In the compound instruction, first the instruction s_1 is executed. If s_1 triggers an exception, s_2 is not executed, and R_e holds. If s_1 terminates normally, s_2 is executed, and the postcondition of the compound is the postcondition of s_2 . Note that for conditionals, check instructions, and loops, the expression e is syntactically restricted not to trigger an exception, which simplifies the rules significantly.

Assignment Instruction

Fig. 5. Axiomatic Semantics for Basic Instructions

3.2 Routine and Routine Invocation Rules

Routine Invocation. Routine invocations of non-once and once routines are verified based on properties of the the virtual method being called:

$$\mathcal{A} \triangleright \{P\} \quad T:m \quad \{Q_n, Q_e\}$$

$$\mathcal{A} \triangleright \left\{ (y \neq Void \land P[y/Current, e/p]) \lor \atop (y = Void \land Q_e) \right\} \quad x := y.T:m(e) \quad \{Q_n[x/Result], Q_e\}$$

In this rule, if the target y must not be Void, the current object is replaced by y and the formal parameter p by the expression e in the precondition P.

Then, in the postcondition Q_n , Result is replaced by x to assign the result of the invocation. If y is Void the invocation triggers and exception, and Q_e holds.

To prove a triple for a virtual method T:m, one has to derive the property for all possible implementations, that is, impl(m, T) and S:m for all sublasses S of T. The corresponding rule is identical to the logic we extend [18].

Routine Implementation. The following rule is used to derive properties of routine implementations from their bodies.

Eiffel pre and postconditions are often too weak for verification, for instance because they cannot contain quantifiers. Therefore, our logic allows one to use stronger conditions. To handle recursion, we add the assumption $\{P\}$ T@m(p) $\{Q_n, Q_e\}$ to the set of routine annotations \mathcal{A} .

3.3 Exception Handling

The operational semantics presented in Section 2.3 shows that a **rescue** clause is a loop. The loop body s_2 ; s_1 iterates until no exception is thrown in s_1 , or *Retry* is false. To be able to reason about this loop, we introduce an invariant I_r . We call this invariant *rescue invariant*. The rule is defined as follows:

$$\begin{array}{c} P \Rightarrow I_{r} \\ \mathcal{A} \triangleright \left\{ I_{r} \right\} \ s_{1} \ \left\{ Q_{n} \ , \ Q_{e} \right\} \\ \hline \mathcal{A} \triangleright \left\{ Q_{e} \right\} \ s_{2} \ \left\{ Retry \Rightarrow I_{r} \ \land \ \neg Retry \Rightarrow R_{e} \ , \ R_{e} \right\} \\ \hline \mathcal{A} \triangleright \left\{ P \right\} \ s_{1} \ \text{rescue} \ s_{2} \ \left\{ Q_{n} \ , \ R_{e} \right\} \end{array}$$

This rule is applied to any routine with a rescue clause. If the do block, s_1 , terminates normally then the rescue block is not executed and the postcondition is Q_n . If s_1 triggers an exception, the rescue block executes. If the rescue block, s_2 , terminates normally, and the Retry variable is true then control flow transfers back to the beginning of the routine and I_r holds. If s_2 terminates normally and Retry is false, the routine triggers an exception and R_e holds. If both s_1 and s_2 trigger an exception, the last one takes precedence, and R_e holds.

3.4 Once Routines

To define the logic for once routines, we use the global variables $T@m_done$, $T@m_result$, and $T@m_exc$, which store if the once routine was executed before or not, the result, and the exception. Let P be the following precondition, where T_M_RES is a logical variable:

$$P \equiv \left\{ \begin{array}{l} (\neg T@m_done \land P') \lor \\ \left(T@m_done \land P'' \land T@m_result = T_M_RES \land \neg T@m_exc \right) \lor \\ \left(T@m_done \land P''' \land T@m_exc \right) \end{array} \right\}$$

and let Q'_n and Q'_e be the following postconditions:

$$Q'_{n} \equiv \left\{ \begin{array}{l} T@m_done \ \land \ \neg T@m_exc \ \land \\ \left(Q_{n} \lor \left(P'' \ \land \ Result = T_M_RES \ \land \ T@m_result = T_M_RES \ \right) \right) \end{array} \right\}$$

$$Q'_{e} \equiv \left\{ \begin{array}{l} T@m_done \ \land \ T@m_exc \ \land \ \left(Q_{e} \ \lor P'''\right) \right\}$$

The rule for once functions is defined as follows:

$$\mathcal{A}, \{P\} \quad T@m \; \{Q'_n, \; Q'_e\} \geqslant$$

$$\left\{ \begin{array}{cccc} P'[false/T@m_done] \wedge & T@m_done \\ \end{array} \right\} \quad body(T@m) \quad \left\{ \begin{array}{cccc} Q_n \; , \; Q_e \\ \end{array} \right\}$$

$$\mathcal{A} \geqslant \left\{ \begin{array}{cccc} P \\ \end{array} \right\} \quad T@m \quad \left\{ \begin{array}{cccc} Q'_n \; , \; Q'_e \\ \end{array} \right\}$$

In the precondition of the body of T@m, $T@m_done$ is true to model recursive call as illustrated in the example presented in Section 2.3. In the postcondition of the rule, under normal termination, either the function T@m is executed and Q_n holds, or the function is not executed since it was already executed and P'' holds. In both cases, $T@m_done$ is true and $T@m_exc$ false. In the case an exception is triggered, $Q_e \vee P'''$ holds.

4 Example

Figure 6 presents an example of the application of the logic. The function $safe_division$ implements an integer division which always terminates normally. If the second operand, y, is zero, this function returns the first operand, x; otherwise it returns the integer division x//y. This function is implemented in Eiffel using a rescue clause. If the division triggers an exception, this exception is handled by the rescue block setting z to 1 and retrying.

To verify this example, we first apply the routine implementation rule (Section 3.2). Then, we apply the rescue rule (Section 3.3) to verify the rescue block. The retry invariant is $(y \neq 0 \land z = 0) \lor (y = 0 \land (z = 1 \lor z = 0))$. Finally, we verify the body of the do block and the body of the rescue block using the assignment, and the compound rule.

5 Soundness and Completeness

We have proved soundness and completeness of the logic. The soundness proof runs by induction on the structure of the derivation tree for $\{P\}$ s $\{Q_n, Q_e\}$. The completeness proof runs by induction on the structure of the instruction s using a sequent which contains a complete specification for every routine implementation T@m. In this section, we state the theorems. The proofs are presented in a technical report [11].

```
1 safe\_division (x, y: INTEGER): INTEGER
         local
 3
              z: INTEGER
         do
              \{ (y \neq 0 \land z = 0) \lor (y = 0 \land (z = 1 \lor z = 0)) \}
 5
              \begin{aligned} & \mathbf{Result} := x \: / / \: (y+z) \\ & \left\{ \left( \begin{matrix} (y=0 \Rightarrow Result = x) \: \land \\ (y \neq 0 \Rightarrow Result = x/y) \end{matrix} \right), (y=0 \land z=0) \right\} \end{aligned} 
         ensure
 9
              zero: y = 0 implies Result = x
              not\_zero: y /= 0 \text{ implies Result} = x // y
11
              \{ y = 0 \land z = 0 \}
13
              z := 1
              \{ (y = 0 \land z = 1), false \}
15
              Retry := true
                \{(Retry \land (y = 0 \land z = 1)), false\}
17
```

Fig. 6. Example of an Eiffel source proof.

```
Definition 3. The triple \models \{P\} s \{Q_n, Q_e\} if and only if:
for all \sigma \models P : \langle \sigma, s \rangle \rightarrow \sigma', \chi then
-\chi = normal \Rightarrow \sigma' \models Q_n, \text{ and}
-\chi = exc \Rightarrow \sigma' \models Q_e
Theorem 1 (Soundness Theorem)
\models \{P\} \quad s \quad \{Q_n, Q_e\} \Rightarrow \models \{P\} \quad s \quad \{Q_n, Q_e\}
Theorem 2 (Completeness Theorem)
\models \{P\} \quad s \quad \{Q_n, Q_e\} \Rightarrow \triangleright \{P\} \quad s \quad \{Q_n, Q_e\}
```

6 Related Work

Huisman and Jacobs [4] have developed a Hoare-style logic with abrupt termination. It includes not only exception handling but also while loops which may contain exceptions, breaks, continues, returns and side-effects. The logic is formulated in a general type theoretical language and not in a specific language such as PVS or Isabelle. Oheimb [23] has developed a Hoare-style calculus for a subset of JavaCard. The language includes side-effecting expressions, mutual recursion, dynamic method binding, full exception handling and static class initialization. These logics formalize a Java-like exception handling which is different to the exception handling presented in this paper.

Logics such as separation logic [20, 13], dynamic frames [5, 22], and regions [1] have been proposed to solve a key issue for reasoning about imperative programs: framing. Separation logic has been adapted to verify object-oriented programs [14, 15, 3]. Parkinson and Bierman [14, 15] introduce abstract predicates: a powerful means to abstract from implementation details and to support information hiding and inheritance. Distefano and Parkinson [3] develop a tool to verify Java programs based on the ideas of abstract predicates.

Logics have been also developed for bytecode languages. Bannwart and Müller [2] have developed a Hoare-style logic a bytecode similar to Java Bytecode and CIL. This logic is based on Poetzsch-Heffter and Müller's logic [17, 18], and it supports object-oriented features such as inheritance and dynamic binding. The Mobius project [9] has also developed a program logic for bytecodes. This logic has been proved sound with respect the operational semantics, and it has been formalized in Coq.

With the goal of verifying bytecode programs, Pavlova [16] has developed an operational semantics, and a verification condition generator (VC) for Java Bytecode. Furthermore, she has shown the equivalence between the verification condition generated from the source program and the one generated from the bytecode. Furthermore, Müller and Nordio [10] present a logic for Java and its proof-transformation for programs with abrupt termination. The language considered includes instructions such as while, try-catch, try-finally, throw, and break.

An operational semantics and a verification methodology for Eiffel has been presented by Schöller [21]. The methodology uses dynamic frame contracts to be able to address the frame problem, and applies to a substantial subset of Eiffel. However, Schöller's work only presents an operational semantics, and it does not include exceptions.

Our logic is based on Poetzsch-Heffter and Müller's work [17, 18], which we extended by new rules for Eiffel instructions. The new rules support Eiffel's exception handling, once routines, and multiple inheritance. This work is based on our earlier effort [12] on proof-transforming compilation from Eiffel to CIL. In this earlier work, we have developed an axiomatic semantics for the exception handling mechanism, and its proof transformation to CIL. This earlier work does not present the operational semantics, and the logic was neither proved sound nor complete. Furthermore, once routines and multiple inheritance were not covered.

7 Lessons Learned

We have presented a sound and complete logic for a subset of Eiffel. Here we report on some lessons on programming language design learned in the process.

Exception Handling. During the development of this work, we have formalized the current Eiffel exception handling mechanism. In the current version of Eiffel, retry is an instruction that can only be used in a rescue block. When

retry is executed, the control flow is transferred to the beginning of the routine. If the execution of the rescue block finishes without invoking a retry, an exception is triggered. Developing a logic for the current Eiffel would require the addition of a third postcondition, to model the execution of retry (since retry is another way of transferring control flow). Thus, we would use Hoare triples of the form $\{P\}$ s $\{Q_n, Q_r, Q_e\}$ where s is an instruction, Q_n is the postcondition under normal termination, Q_r the postcondition after the execution of a retry, and Q_e the exceptional postcondition.

Such a formalization would make verification harder than with the formalization we use in this paper, because the extra postcondition required by the retry instruction would have to be carried throughout the whole reasoning. In this paper, we have observed that a rescue block behaves as a loop that iterates until no exception is triggered, and that retry can be modeled simply as a variable which guards the loop. Since the retry instruction transfers control flow to the beginning of the routine, a retry instruction has a similar behavior to a continue in Java or C#. Our proposed change of the retry instruction to a variable will be introduced in the next revision of the language standard [8].

Since Eiffel does not have return instructions, nor continue, nor break instructions, Eiffel programs can be verified using Hoare triples with only two postconditions. To model object-oriented programs with abrupt termination in languages such as Java or C#, one needs to introduce extra postconditions for return, break or continue (or we could introduce a variable to model abrupt termination). If we wanted to model the current version of Java, for example, we would also need to add postconditions for labelled breaks and labelled continues. Thus, one would need to add as many postcondition as there are labels in the program. These features for abrupt termination make the logic more complex and harder to use.

Another difference between Eiffel and Java and C# is that Eiffel supports exceptions using rescue clauses, and Java and C# using try-catch and try-finally instructions. The use of try-finally makes the logic harder as pointed out by Müller and Nordio [10]. The combination of try-finally and break instructions makes the rules more complex and harder to apply because one has to consider all possible cases in which the instructions can terminate (normal, break, return, exception, etc).

However, we cannot conclude that the Eiffel's exception handling mechanism is always simpler for verification; although it eliminates the problems produced by try-finally, break, and return instructions. Since the rescue block is a loop, one needs a retry invariant. When the program is simple, and it does not trigger many different exceptions, defining this retry invariant is simple. But, if the program triggers different kinds of exception at different locations, finding this invariant can be more complicated. Note that finding this retry invariant is more complicated than finding a loop invariant since in a loop invariant one has to consider only normal termination (and in Java and C#, also continue instructions), but in retry invariants one needs to consider all possible executions and all possible exceptions.

Multiple Inheritance. Introducing multiple inheritance to a programing language is not an easy task. The type system has to be extended, and this extension is complex. However, since the resolution of a routine name can be done syntactically, extending Poetzsch-Heffter and Müller's logic [18] to handle multiple inheritance was not a complicated task. The logic was easily extended by giving a new definition of the function impl. This function returns the body of a routine by searching the definition in the parent classes, and considering the clauses redefine, undefine, and rename. The experience with this paper indicates that the complexity of a logic for multiple inheritance is similar to a logic for single inheritance.

Once Routines. To verify once routines, we introduce global variables to express whether the once routine has been executed before or not, and whether the routine triggered an exception or not. With the current mechanism, the use of recursion in once functions does not increase the expressivity of the language. In fact, every recursive call can be equivalently replaced by *Result*. However, the rule for once functions is more complicated than it could be if recursion were omitted.

Recursive once function would be more interesting if we changed the semantics of once routines. Instead of setting the global variable done before the execution of the body of the once function, we could set it after the invocation. Then the recursive once function would be invoked until the last recursive call finishes. Thus, for example, the result of the first invocation of factorial(n) would be n! (the function factorial is presented in Section 2.3). Later invocations of factorial would return the stored result. However, this change would not simplify the logic, and we would need to use global variables to mark whether the once function was invoked before or not.

Analyzing the EiffelBase libraries, and the source code of the EiffelStudio compiler, we found that the predominant use of once functions is without arguments, which makes sense because arguments of subsequent calls are meaningless. Even though our rules for once functions are not overly complicated, verification of once functions is cumbersome because one has to carry around the outcome of the first invocation in proofs. It is unclear whether this is any simpler than reasoning about static methods and fields [6].

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